# Vibrational and quantum chemical analysis of 3-methyl-2,6-diphenyl piperidin-4-one using HF and DFT methods 

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#### Abstract

Characterization of 3-methyl-2,6-diphenylpiperidin-4-one (MDPO) by quantum chemical calculations and spectral techniques has been performed with spectroscopic investigations like FT-IR, FT-Raman and UV techniques. Molecular geometries, FT-IR spectrum ( $4000-400 \mathrm{~cm}^{-1}$ ) and FT-Raman spectrum ( $4000-100 \mathrm{~cm}^{-1}$ ) in solid phase was recorded. The structural and spectroscopic data of the molecule were obtained from HF and B3LYP with $6-311++\mathrm{G}(\mathrm{d}, \mathrm{p})$ levels using density functional theory (DFT). The stability and intra-molecular charge transfer have been analyzed by the detailed natural bond orbital (NBO) analysis. The charge transfer occurring in the molecule was verified and found to be stable from smaller energy gap by HOMO-LUMO analysis. Atomic population analysis reveals the percentage of electron distribution in s -and p-subshells. The first order hyperpolarizability of the investigated molecule has been studied theoretically. The calculated results were applied to simulated infrared and Raman spectra of the title molecule which show good agreement with observed spectra.


Keywords: DFT, HOMO, LUMO, Natural Bond Orbital, Hyperpolarizability, UV spectra

## 1 Introduction

Piperidine derivatives were found to possess pharmacological activity. They are the essential part of molecular structures in important drugs ${ }^{1}$. Piperidone derivatives as prospective biophotonic materials has been explored recently. Piperidines form an important framework and served as precursors for chiral biologically active natural alkaloids. Their biological activity is excellent if 2-and/or 6-positions are occupied by aryl groups. Its anti-bacterial and anti-fungal activities have been explored well. 2,6diaryl piperidine4-one have been subjected to quite a large number of synthetic and physico-chemical studies.Piperidine-4-one pharmacophore is present in a wide variety of naturally occurring alkaloids and is responsible for a number of biological actions such as anti-bacterial, anti-fungal, anti-tuberchlostic, anti-cancer,anti-oxidant, anti-inflammatory neuronal nicotinic antagonistic activity, CNS stimulant, depressant ${ }^{2-6}$. Miglitol, a piperidine derivative, is primarily used in diabetes mellitus type-2 for establishing greater glycemic control by preventing the digestion of carbohydrates into monosaccharides which can be absorbed by body ${ }^{7}$. Piperidine is used as
a rubber vulcanization accelerator. In pharmaceutical synthesis industry, it is a special solvent and as a protecting group for peptide synthesis. Piperidine derivative compounds are used as intermediate to make crystal derivative of aromatic nitrogen compounds containing nuclear halogen atoms. It is a structural element for pharma drugs like raloxifene and minoxidil. Ring system compounds with nitrogen which have basic properties play important role as cyclic compounds in the industrial field such as raw materials for hardness of epoxy resins, corrosion inhibitors, insecticides, accelerators for rubber, urethane catalysts, anti-oxidants and as a catalyst for silicone esters ${ }^{8}$. The theoretical ab-initio, DFT, and spectroscopical analysis of the title molecule give information regarding the nature of the electronic structure, the functional groups and orbital interactions and mixing of vibrational frequencies ${ }^{36-38}$.

## 2 Experimental Details

### 2.1 Synthesis of MDPO

To a solution of dry ammonium acetate ( 9.8 g , 0.125 mol ) in glacial acetic acid ( $12.5 \mathrm{~g}, 0.21 \mathrm{~mol}$ ) was added benzaldehyde ( $29 \mathrm{~g}, 0.25 \mathrm{~mol}$ ) and
butanone ( $9 \mathrm{~g}, 0.125 \mathrm{~mol}$ ). The mixture was just heated to boil and allowed to stand overnight at room temperature. The concentrated hydrochloric acid $(13 \mathrm{ml})$ was added, the precipitated hydrochloride was collected and washed with ethanol-ether (1:5) mixture. Crystallization from ethanol-ether yielded the pure hydrochloride, mp $\left(223-225^{\circ} \mathrm{C}\right)$ (lit 224$226^{\circ} \mathrm{C}$ )

A suspension of the hydrochloride in acetone was treated with ammonia (1:1) and the free base was obtained by diluting with large amount of water. Crystallization of the product from ethanol ${ }^{39,40}$ gave 3-methyl-2,6-diphenylpiperidin-4-one $\operatorname{mp}\left(96-97^{\circ} \mathrm{C}\right)$ (lit $96-97^{\circ} \mathrm{C}$ ).

### 2.2 FT-Raman and FT-IR measurement

FT-Raman spectrum of MDPO was recorded using ND: YAG laser as excitation wavelength in the region $50-4000 \mathrm{~cm}^{-1}$ using BRUKER RFS 27 standalone spectrometer. The ND:YAG laser source operates at 1064 nm line with 200 mW powers. The FT-IR spectrum of the MDPO was recorded using PERKINELMER spectrometer in the region $4000-100 \mathrm{~cm}^{-1}$. The frequencies of all sharp bands are accurate to $\pm 1 \mathrm{~cm}^{-1}$.

## 3 Computational Details

The molecular geometry optimization and vibrational frequency calculations were carried out for MDPO using GAUSSIAN 09 software ${ }^{9}$. HFfunctional ${ }^{10,11}$ combined with standard basis set HF/6-311++G(d,p) and denstity functional method B3LYP/6-31++G(d,p) used is B3LYP i.e., Becke's three-parameter hybrid functional with Lee-Yang-Parr correlation method ${ }^{12,13}$. The Raman activities ( $\mathrm{S}^{\mathrm{A}}$ ) calculated with Gaussian 09 program were converted to relative Raman intensities ( $I^{\mathrm{RA}}$ ) using the following relationship derived from the intensity theory of Raman scattering ${ }^{14,15}$.
$I_{R A}=\frac{f\left(v_{o}-v_{i}\right)^{4} S_{i}}{v_{i}\left[1-\exp \left(-h c v_{i} / k t\right)\right]}$
where $v_{o}$ is the exciting frequency in $\mathrm{cm}^{-1}, v_{i}$ the vibrational wavenumber of the $\left(i^{t h}\right)$ normal mode, $h, c$ and $k$ are fundamental constants.

## 4 Results and Discussion

### 4.1 Moecular Geometry

The bond lengths and bond angles of MDPO are given in Table 1. The optimized structure of MDPO

Table 1 - Bond lengths. bond angles, torsional angles and dihedral angles of MDPO

| Bond length ( $\AA$ ) | $\begin{gathered} \text { HF } \\ 6-311++\mathrm{G}(\mathrm{~d}, \mathrm{p}) \end{gathered}$ | $\begin{gathered} \text { B3LYP } \\ 6-311++G(d, p) \end{gathered}$ |
| :---: | :---: | :---: |
| $\mathrm{N}_{1}-\mathrm{C}_{2}$ | 1.4696 | 1.4863 |
| $\mathrm{N}_{1}-\mathrm{C}_{6}$ | 1.4551 | 1.4749 |
| $\mathrm{N}_{1}-\mathrm{H}_{21}$ | 0.9977 | 1.0118 |
| $\mathrm{C}_{2}-\mathrm{C}_{3}$ | 1.5500 | 1.5662 |
| $\mathrm{C}_{2}-\mathrm{C}_{15}$ | 1.5240 | 1.5256 |
| $\mathrm{C}_{2}-\mathrm{H}_{22}$ | 1.0859 | 1.0954 |
| $\mathrm{C}_{3}-\mathrm{C}_{4}$ | 1.5206 | 1.5215 |
| $\mathrm{C}_{3}-\mathrm{C}_{8}$ | 1.5247 | 1.5302 |
| $\mathrm{C}_{3}-\mathrm{H}_{23}$ | 1.0900 | 1.0993 |
| $\mathrm{C}_{4}-\mathrm{C}_{5}$ | 1.5171 | 1.5156 |
| $\mathrm{C}_{4}-\mathrm{O}_{7}$ | 1.1881 | 1.2409 |
| $\mathrm{C}_{5}-\mathrm{C}_{6}$ | 1.5308 | 1.5411 |
| $\mathrm{C}_{5}-\mathrm{H}_{24}$ | 1.0843 | 1.0927 |
| $\mathrm{C}_{5}-\mathrm{H}_{25}$ | 1.0864 | 1.0945 |
| $\mathrm{C}_{6}-\mathrm{C}_{9}$ | 1.5189 | 1.5216 |
| $\mathrm{C}_{6}-\mathrm{H}_{26}$ | 1.0912 | 1.1031 |
| $\mathrm{C}_{8}-\mathrm{H}_{27}$ | 1.0829 | 1.0893 |
| $\mathrm{C}_{8}-\mathrm{H}_{28}$ | 1.0851 | 1.0915 |
| $\mathrm{C}_{8}-\mathrm{H}_{29}$ | 1.0840 | 1.0902 |
| $\mathrm{C}_{9}-\mathrm{C}_{10}$ | 1.3875 | 1.4018 |
| $\mathrm{C}_{9}-\mathrm{C}_{14}$ | 1.3922 | 1.4039 |
| $\mathrm{C}_{10}-\mathrm{C}_{11}$ | 1.3877 | 1.3985 |
| $\mathrm{C}_{10}-\mathrm{H}_{30}$ | 1.0766 | 1.0840 |
| $\mathrm{C}_{11}-\mathrm{C}_{12}$ | 1.3828 | 1.3971 |
| $\mathrm{C}_{11}-\mathrm{H}_{31}$ | 1.0756 | 1.0824 |
| $\mathrm{C}_{12}-\mathrm{C}_{13}$ | 1.3873 | 1.3991 |
| $\mathrm{C}_{12}-\mathrm{H}_{32}$ | 1.0754 | 1.0822 |
| $\mathrm{C}_{13}-\mathrm{C}_{14}$ | 1.3836 | 1.3968 |
| $\mathrm{C}_{13}-\mathrm{H}_{33}$ | 1.0757 | 1.0825 |
| $\mathrm{C}_{14}-\mathrm{H}_{34}$ | 1.0745 | 1.0817 |
| $\mathrm{C}_{15}-\mathrm{C}_{16}$ | 1.3869 | 1.4015 |
| $\mathrm{C}_{15}-\mathrm{C}_{20}$ | 1.3935 | 1.4051 |
| $\mathrm{C}_{16}-\mathrm{C}_{17}$ | 1.3886 | 1.3990 |
| $\mathrm{C}_{16}-\mathrm{C}_{35}$ | 1.0761 | 1.0834 |
| $\mathrm{C}_{17}-\mathrm{C}_{18}$ | 1.3820 | 1.3965 |
| $\mathrm{C}_{17}-\mathrm{H}_{36}$ | 1.0756 | 1.0824 |
| $\mathrm{C}_{18}-\mathrm{C}_{19}$ | 1.3879 | 1.3997 |
| $\mathrm{C}_{18}-\mathrm{H}_{37}$ | 1.0753 | 1.0821 |
| $\mathrm{C}_{19}-\mathrm{C}_{20}$ | 1.3826 | 1.3962 |
| $\mathrm{C}_{19}-\mathrm{H}_{38}$ | 1.0757 | 1.0825 |
| $\mathrm{C}_{20}-\mathrm{H}_{39}$ | 1.0757 | 1.0832 |
| Bond angle (degrees) |  |  |
| $\mathrm{C}_{2}-\mathrm{N}_{1}-\mathrm{C}_{6}$ | 118.1421 | 119.5862 |
| $\mathrm{C}_{2}-\mathrm{N}_{1}-\mathrm{H}_{21}$ | 110.7908 | 112.8618 |
| $\mathrm{C}_{6}-\mathrm{N}_{1}-\mathrm{H}_{21}$ | 111.2114 | 113.3203 |
| $\mathrm{N}_{1}-\mathrm{C}_{2}-\mathrm{C}_{3}$ | 111.7473 | 110.8473 |
| $\mathrm{N}_{1}-\mathrm{C}_{2}-\mathrm{C}_{15}$ | 112.3014 | 112.0902 |
| $\mathrm{N}_{1}-\mathrm{C}_{2}-\mathrm{H}_{22}$ | 107.1556 | 108.1676 |
| $\mathrm{C}_{3}-\mathrm{C}_{2}-\mathrm{C}_{15}$ | 112.1656 | 111.9976 |
| $\mathrm{C}_{3}-\mathrm{C}_{2}-\mathrm{H}_{22}$ | 106.3564 | 106.1665 |
| $\mathrm{C}_{15}-\mathrm{C}_{2}-\mathrm{H}_{22}$ | 106.6641 | 107.2517 |
| $\mathrm{C}_{2}-\mathrm{C}_{3}-\mathrm{C}_{4}$ | 109.4959 | 109.5225 |
| $\mathrm{C}_{2}-\mathrm{C}_{3}-\mathrm{C}_{8}$ | 112.8051 | 112.5910 |
| $\mathrm{C}_{2}-\mathrm{C}_{3}-\mathrm{H}_{23}$ | 107.9987 | 107.0186 |

Table 1 — | Bond lengths. bond angles, torsional angles and |
| :---: |
| dihedral angles of MDPO - Contd |

| Bond length ( $\AA$ ) | $\begin{gathered} \text { HF } \\ 6-311++\mathrm{G}(\mathrm{~d}, \mathrm{p}) \end{gathered}$ | $\begin{gathered} \text { B3LYP } \\ 6-311++G(d, p) \end{gathered}$ | Bond length ( $\AA$ ) | $\begin{gathered} \text { HF } \\ 6-311++\mathrm{G}(\mathrm{~d}, \mathrm{p}) \end{gathered}$ | $\begin{gathered} \text { B3LYP } \\ 6-311++G(d, p) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{C}_{4}-\mathrm{C}_{3}-\mathrm{C}_{8}$ | 112.3059 | 112.6547 | $\mathrm{C}_{18}-\mathrm{C}_{19}-\mathrm{H}_{38}$ | 120.0133 | 120.0040 |
| $\mathrm{C}_{4}-\mathrm{C}_{3}-\mathrm{H}_{23}$ | 105.0768 | 105.7638 | $\mathrm{C}_{20}-\mathrm{C}_{19}-\mathrm{H}_{38}$ | 119.7503 | 119.8392 |
| $\mathrm{C}_{8}-\mathrm{C}_{3}-\mathrm{H}_{23}$ | 108.7786 | 108.9064 | $\mathrm{C}_{15}-\mathrm{C}_{20}-\mathrm{C}_{19}$ | 120.9152 | 120.7720 |
| $\mathrm{C}_{3}-\mathrm{C}_{4}-\mathrm{C}_{5}$ | 115.6936 | 116.5321 | $\mathrm{C}_{15}-\mathrm{C}_{20}-\mathrm{H}_{39}$ | 120.1144 | 119.7788 |
| $\mathrm{C}_{3}-\mathrm{C}_{4}-\mathrm{O}_{7}$ | 122.9754 | 122.3938 | $\mathrm{C}_{19}-\mathrm{C}_{20}-\mathrm{H}_{39}$ | 118.9702 | 119.4481 |
| $\mathrm{C}_{5}-\mathrm{C}_{4}-\mathrm{O}_{7}$ | 121.3272 | 121.0714 | Torsion angles (degrees) |  |  |
| $\mathrm{C}_{4}-\mathrm{C}_{5}-\mathrm{C}_{6}$ | 112.1782 | 112.5808 |  |  |  |
| $\mathrm{C}_{4}-\mathrm{C}_{5}-\mathrm{H}_{24}$ | 107.2525 | 107.8247 | $\mathrm{C}_{5}-\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{14}$ $\mathrm{C}_{5}-\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{10}$ | 74.6653 -104.0817 | $\begin{gathered} 73.8556 \\ -104.7629 \end{gathered}$ |
| $\mathrm{C}_{4}-\mathrm{C}_{5}-\mathrm{H}_{25}$ | 108.1954 | 108.7911 | $\mathrm{C}_{5}-\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{10}$ $\mathrm{C}_{3}-\mathrm{C}_{2}-\mathrm{C}_{15}-\mathrm{C}_{20}$ | $\begin{gathered} -104.0817 \\ 66.7939 \end{gathered}$ | $\begin{gathered} -104.7629 \\ 69.6542 \end{gathered}$ |
| $\mathrm{C}_{6}-\mathrm{C}_{5}-\mathrm{H}_{24}$ | 110.4382 | 109.8381 | $\mathrm{C}_{3}-\mathrm{C}_{2}-\mathrm{C}_{15}-\mathrm{C}_{20}$ $\mathrm{C}_{3}-\mathrm{C}_{2}-\mathrm{C}_{15}-\mathrm{C}_{16}$ | -114.1878 | $\begin{gathered} 69.6542 \\ -111.005 \end{gathered}$ |
| $\mathrm{C}_{6}-\mathrm{C}_{5}-\mathrm{H}_{25}$ | 111.3081 | 110.9411 | $\mathrm{C}_{3}-\mathrm{C}_{2}-\mathrm{C}_{15}-\mathrm{C}_{16}$ $\mathrm{C}_{2}-\mathrm{N}_{1}-\mathrm{C}_{6}-\mathrm{C}_{9}$ | -114.1878 | $\begin{array}{r} -111.005 \\ 179.8656 \end{array}$ |
| $\mathrm{H}_{24}-\mathrm{C}_{5}-\mathrm{H}_{25}$ | 107.2536 | 106.6426 | $\mathrm{C}_{2}-\mathrm{N}_{1}-\mathrm{C}_{6}-\mathrm{C}_{9}$ $\mathrm{C}_{6}-\mathrm{N}_{1}-\mathrm{C}_{2}-\mathrm{C}_{15}$ | -176.3563 | $114.8109$ |
| $\mathrm{N}_{1}-\mathrm{C}_{6}-\mathrm{C}_{5}$ | 107.5251 | 107.4809 | $\mathrm{C}_{6}-\mathrm{N}_{1}-\mathrm{C}_{2}-\mathrm{C}_{15}$ $\mathrm{C}_{4}-\mathrm{C}_{5}-\mathrm{C}_{6}-\mathrm{N}_{1}$ | -46.7674 | 114.8109 |
| $\mathrm{N}_{1}-\mathrm{C}_{6}-\mathrm{C}_{9}$ | 110.5987 | 110.4269 | $\mathrm{C}_{4}-\mathrm{C}_{5}-\mathrm{C}_{6}-\mathrm{N}_{1}$ $\mathrm{C}_{1}-\mathrm{C}_{2}-\mathrm{C}_{3}-\mathrm{C}_{4}$ | -46.7674 -39.9585 | -46.8936 -42.5899 |
| $\mathrm{N}_{1}-\mathrm{C}_{6}-\mathrm{H}_{26}$ | 112.0906 | 112.0933 | $\mathrm{C}_{1}-\mathrm{C}_{2}-\mathrm{C}_{3}-\mathrm{C}_{4}$ $\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{14}-\mathrm{C}_{13}$ | -39.9585 | -42.5899 |
| $\mathrm{C}_{5}-\mathrm{C}_{6}-\mathrm{C}_{9}$ | 111.8117 | 111.9792 | $\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{14}-\mathrm{C}_{13}$ $\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{14}-\mathrm{C}_{34}$ | -178.5754 1.8512 | -178.3154 |
| $\mathrm{C}_{5}-\mathrm{C}_{6}-\mathrm{H}_{26}$ | 108.2941 | 108.0919 | $\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{14}-\mathrm{C}_{34}$ $\mathrm{C}_{2}-\mathrm{C}_{15}-\mathrm{C}_{16}-\mathrm{C}_{17}$ | 1.8512 -179.5186 | 2.3174 -179.8502 |
| $\mathrm{C}_{9}-\mathrm{C}_{6}-\mathrm{H}_{26}$ | 106.5525 | 106.8026 | ${ }_{\mathrm{C}_{2}}-\mathrm{C}_{15}-\mathrm{C}_{16}-\mathrm{C}_{17}$ | -179.5186 0.4216 | -179.8502 -0.0212 |
| $\mathrm{C}_{3}-\mathrm{C}_{8}-\mathrm{H}_{27}$ | 110.3982 | 110.5885 | $\mathrm{C}_{2}-\mathrm{C}_{15}-\mathrm{C}_{16}-\mathrm{C}_{35}$ $\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{10}-\mathrm{H}_{30}$ | 0.4216 -1.6909 | -0.0212 -1.9074 |
| $\mathrm{C}_{3}-\mathrm{C}_{8}-\mathrm{H}_{28}$ | 110.9205 | 110.8816 | $\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{10}-\mathrm{H}_{30}$ $\mathrm{C}_{2}-\mathrm{C}_{15}-\mathrm{C}_{20}-\mathrm{H}_{39}$ | -1.6909 -0.4061 | -1.9074 0.2254 |
| $\mathrm{C}_{3}-\mathrm{C}_{8}-\mathrm{H}_{29}$ | 110.7194 | 110.7238 | $\mathrm{C}_{2}-\mathrm{C}_{15}-\mathrm{C}_{20}-\mathrm{H}_{39}$ $\mathrm{C}_{2}-\mathrm{C}_{15}-\mathrm{C}_{20}-\mathrm{C}_{19}$ | -0.4061 179.4228 | 179.8334 |
| $\mathrm{H}_{27}-\mathrm{C}_{8}-\mathrm{H}_{28}$ | 107.4610 | 107.1649 | $\mathrm{C}_{2}-\mathrm{C}_{15}-\mathrm{C}_{20}-\mathrm{C}_{19}$ $\mathrm{~N}_{1}-\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{10}$ | 179.4228 136.1223 | 179.8334 |
| $\mathrm{H}_{27}-\mathrm{C}_{8}-\mathrm{H}_{29}$ | 108.6149 | 108.7638 | $\mathrm{N}_{1}-\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{10}$ $\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{10}-\mathrm{C}_{11}$ | 136.1223 178.3901 | 135.5026 178.1592 |
| $\mathrm{H}_{28}-\mathrm{C}_{8}-\mathrm{H}_{29}$ | 108.6294 | 108.6131 | $\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{10}-\mathrm{C}_{11}$ $\mathrm{~N}_{1}-\mathrm{C}_{2}-\mathrm{C}_{3}-\mathrm{C}_{8}$ | $-165.8068$ | $\begin{gathered} 178.1592 \\ -168.7582 \end{gathered}$ |
| $\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{10}$ | 120.1457 | 120.3219 | $\mathrm{N}_{1}-\mathrm{C}_{2}-\mathrm{C}_{3}-\mathrm{C}_{8}$ $\mathrm{C}_{2}-\mathrm{N}_{1}-\mathrm{C}_{6}-\mathrm{C}_{9}$ | $\begin{aligned} & -165.8068 \\ & -176.3563 \end{aligned}$ | $\begin{gathered} -168.7582 \\ 179.8656 \end{gathered}$ |
| $\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{14}$ | 121.2441 | 120.8708 | $\mathrm{C}_{2}-\mathrm{N}_{1}-\mathrm{C}_{6}-\mathrm{C}_{9}$ | -176.3563 | 179.8656 |
| $\mathrm{C}_{10}-\mathrm{C}_{9}-\mathrm{C}_{14}$ | 118.5987 | 118.7933 | Dihedral angles(degrees) |  |  |
| $\mathrm{C}_{9}-\mathrm{C}_{10}-\mathrm{C}_{11}$ | 120.9245 | 120.7747 |  |  |  |
| $\mathrm{C}_{9}-\mathrm{C}_{10}-\mathrm{H}_{30}$ | 119.7477 | 119.5087 | $\mathrm{C}_{8}-\mathrm{C}_{3}-\mathrm{C}_{4}-\mathrm{C}_{5}$ | 177.9677 | 177.4545 |
| $\mathrm{C}_{11}-\mathrm{C}_{10}-\mathrm{H}_{30}$ | 119.3277 | 119.7166 | $\mathrm{C}_{3}-\mathrm{C}_{4}-\mathrm{C}_{5}-\mathrm{H}_{24}$ | -128.875 | -126.4792 |
| $\mathrm{C}_{10}-\mathrm{C}_{11}-\mathrm{C}_{12}$ | 120.0437 | 120.0256 | $\mathrm{N}_{1}-\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{14}$ | -45.1307 | -45.8789 |
| $\mathrm{C}_{10}-\mathrm{C}_{11}-\mathrm{H}_{31}$ | 119.7670 | 119.8408 | $\mathrm{C}_{2}-\mathrm{C}_{3}-\mathrm{C}_{4}-\mathrm{O}_{7}$ | -128.8635 | -129.2648 |
| $\mathrm{C}_{12}-\mathrm{C}_{11}-\mathrm{H}_{31}$ | 120.1887 | 120.1331 | $\mathrm{O}_{7}-\mathrm{C}_{4}-\mathrm{C}_{5}-\mathrm{C}_{6}$ | 173.2403 | 175.4179 |
| $\mathrm{C}_{11}-\mathrm{C}_{12}-\mathrm{C}_{13}$ | 119.4906 | 119.6218 | $\mathrm{H}_{26}-\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{10}$ | 14.0606 | 13.3812 |
| $\mathrm{C}_{11}-\mathrm{C}_{12}-\mathrm{H}_{32}$ | 120.2803 | 120.1866 | $\mathrm{H}_{26}-\mathrm{C}_{6}-\mathrm{C}_{9}-\mathrm{C}_{14}$ | -167.1925 | -168.0003 |
| $\mathrm{C}_{13}-\mathrm{C}_{12}-\mathrm{H}_{32}$ | 120.2288 | 120.1913 |  |  |  |
| $\mathrm{C}_{12}-\mathrm{C}_{13}-\mathrm{C}_{14}$ | 120.3572 | 120.2687 | BD ${ }^{*}(1) \mathrm{C}_{3}-\mathrm{C}_{4}$ | 0.05258 | 0.63425 |
| $\mathrm{C}_{12}-\mathrm{C}_{13}-\mathrm{H}_{33}$ | 119.9699 | 119.9814 | BD ${ }^{*}(1) \mathrm{C}_{3}-\mathrm{C}_{8}$ | 0.01009 | 0.61706 |
| $\mathrm{C}_{14}-\mathrm{C}_{13}-\mathrm{H}_{33}$ | 119.6729 | 119.7499 | BD* ${ }^{*}$ (1) $\mathrm{C}_{3}-\mathrm{H}_{23}$ | 0.01701 | 0.58065 |
| $\mathrm{C}_{9}-\mathrm{C}_{14}-\mathrm{C}_{13}$ | 120.5842 | 120.5142 | BD* ${ }^{*}(1) \mathrm{C}_{4}-\mathrm{C}_{5}$ | 0.04249 | 0.62741 |
| $\mathrm{C}_{9}-\mathrm{C}_{14}-\mathrm{H}_{34}$ | 119.5295 | 119.1567 | $\mathrm{BD} *{ }^{*}(1) \mathrm{C}_{4}-\mathrm{O}_{7}$ | 0.01229 | 0.86930 |
| $\mathrm{C}_{13}-\mathrm{C}_{14}-\mathrm{H}_{34}$ | 119.8850 | 120.3260 | BD* ${ }^{*}$ (2) $\mathrm{C}_{4}-\mathrm{O}_{7}$ | 0.05680 | 0.20764 |
| $\mathrm{C}_{2}-\mathrm{C}_{15}-\mathrm{C}_{16}$ | 120.1095 | 120.2873 | $\mathrm{BD}^{*}(1) \mathrm{C}_{5}-\mathrm{C}_{6}$ | 0.02336 | 0.61113 |
| $\mathrm{C}_{2}-\mathrm{C}_{15}-\mathrm{C}_{20}$ | 121.6304 | 121.2057 | BD* ${ }^{*}$ (1) $\mathrm{C}_{5}-\mathrm{H}_{24}$ | 0.00906 | 0.60746 |
| $\mathrm{C}_{16}-\mathrm{C}_{15}-\mathrm{C}_{20}$ | 118.2531 | 118.5039 | $\mathrm{BD}^{*}(1) \mathrm{C}_{5}-\mathrm{H}_{25}$ | 0.01174 | 0.58040 |
| $\mathrm{C}_{15}-\mathrm{C}_{16}-\mathrm{C}_{17}$ | 121.0493 | 120.9143 | BD** ${ }^{*} \mathrm{C}_{6}-\mathrm{C}_{9}$ | 0.02540 | 0.68980 |
| $\mathrm{C}_{15}-\mathrm{C}_{16}-\mathrm{H}_{35}$ | 119.5844 | 119.3250 | BD** ${ }^{*} \mathrm{C}_{6}-\mathrm{H}_{26}$ | 0.05674 | 0.62151 |
| $\mathrm{C}_{17}-\mathrm{C}_{16}-\mathrm{H}_{35}$ | 119.3663 | 119.7605 | $\mathrm{BD}^{*}(1) \mathrm{C}_{8}-\mathrm{H}_{27}$ | 0.00461 | 0.60894 |
| $\mathrm{C}_{16}-\mathrm{C}_{17}-\mathrm{C}_{18}$ | 120.1219 | 120.0474 | $\mathrm{BD}^{*}(1) \mathrm{C}_{8}-\mathrm{H}_{28}$ | 0.00616 | 0.60021 |
| $\mathrm{C}_{16}-\mathrm{C}_{17}-\mathrm{H}_{36}$ | 119.7164 | 119.8364 | $\mathrm{BD}^{*}(1) \mathrm{C}_{8}-\mathrm{H}_{29}$ | 0.00473 | 0.59746 |
| $\mathrm{C}_{18}-\mathrm{C}_{17}-\mathrm{H}_{36}$ | 120.1614 | 120.1157 | $\mathrm{BD}^{*}(1) \mathrm{C}_{9}-\mathrm{C}_{10}$ | 0.02106 | 0.79621 |
| $\mathrm{C}_{17}-\mathrm{C}_{18}-\mathrm{C}_{19}$ | 119.4225 | 119.6035 | $\mathrm{BD}^{*}(2) \mathrm{C}_{9}-\mathrm{C}_{10}$ | 0.33779 | 0.16583 |
| $\mathrm{C}_{17}-\mathrm{C}_{18}-\mathrm{H}_{37}$ | 120.3551 | 120.2498 | $\mathrm{BD}^{*}(1) \mathrm{C}_{9}-\mathrm{C}_{14}$ | 0.02327 | 0.79137 |
| $\mathrm{C}_{19}-\mathrm{C}_{18}-\mathrm{H}_{37}$ | 120.2221 | 120.1461 | BD**) $\mathrm{C}_{10}-\mathrm{C}_{11}$ | 0.01238 | 0.78681 |
| $\mathrm{C}_{18}-\mathrm{C}_{19}-\mathrm{C}_{20}$ | 120.2364 | 120.1568 | BD ${ }^{(1)} \mathrm{C}_{10}-\mathrm{H}_{30}$ | 0.01094 | 0.64409 |
|  |  | Contd- |  |  | Contd |


| Table 1 - Bond lengths. bond angles, torsional angles and dihedral angles of MDPO - Contd |  |  |
| :---: | :---: | :---: |
| Bond | HF | B3LYP |
| length( A ) | $6-311++G(d, p)$ | $6-311++G(d, p)$ |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{11}-\mathrm{C}_{12}$ | 0.01348 | 0.78862 |
| $\mathrm{BD}^{*}(2) \mathrm{C}_{11}-\mathrm{C}_{12}$ | 0.32724 | 0.15654 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{11}-\mathrm{H}_{31}$ | 0.01031 | 0.64911 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{12}-\mathrm{C}_{13}$ | 0.01351 | 0.78919 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{12}-\mathrm{H}_{32}$ | 0.01057 | 0.65192 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{13}-\mathrm{C}_{14}$ | 0.01284 | 0.79277 |
| $\mathrm{BD}^{*}(2) \mathrm{C}_{13}-\mathrm{C}_{14}$ | 0.31295 | 0.16319 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{13}-\mathrm{H}_{33}$ | 0.01061 | 0.65130 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{14}-\mathrm{H}_{34}$ | 0.01048 | 0.66030 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{15}-\mathrm{C}_{16}$ | 0.02079 | 0.78368 |
| $\mathrm{BD}^{*}(2) \mathrm{C}_{15}-\mathrm{C}_{16}$ | 0.33061 | 0.15486 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{15}-\mathrm{C}_{20}$ | 0.02516 | 0.77248 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{16}-\mathrm{C}_{17}$ | 0.01252 | 0.77647 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{16}-\mathrm{H}_{35}$ | 0.01099 | 0.63166 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{17}-\mathrm{C}_{18}$ | 0.01329 | 0.77773 |
| $\mathrm{BD}^{*}(2) \mathrm{C}_{17}-\mathrm{C}_{18}$ | 0.32384 | 0.14697 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{17}-\mathrm{H}_{36}$ | 0.01027 | 0.64069 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{18}-\mathrm{C}_{19}$ | 0.01302 | 0.77600 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{18}-\mathrm{H}_{37}$ | 0.01040 | 0.64210 |
| BD* ${ }^{*}$ (1) $\mathrm{C}_{19}-\mathrm{C}_{20}$ | 0.01646 | 0.77983 |
| $\mathrm{BD}^{*}(2) \mathrm{C}_{19}-\mathrm{C}_{20}$ | 0.34482 | 0.14943 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{19}-\mathrm{H}_{38}$ | 0.01037 | 0.63444 |
| $\mathrm{BD}^{*}(1) \mathrm{C}_{20}-\mathrm{H}_{39}$ | 0.01749 | 0.63644 |

along with the atom numbering schemes is shown in Fig. 1. This compound has $\mathrm{N}-\mathrm{H}$ bond, $\mathrm{C}-\mathrm{O}$ bond, $\mathrm{C}-\mathrm{N}$ bonds, $\mathrm{C}-\mathrm{H}$ bonds and $\mathrm{C}-\mathrm{C}$ bonds. $\mathrm{C}_{4}-\mathrm{O}_{7}$ average bond length $1.20 \AA$. $\mathrm{C}-\mathrm{C}$ bond length is usually observed ${ }^{16}$ to be nearly equal to $1.400 \AA$. In the present investigation, bond lengths of $\mathrm{C}_{2}-\mathrm{C}_{3}$, $\mathrm{C}_{2}-\mathrm{C}_{15}, \mathrm{C}_{3}-\mathrm{C}_{4}, \mathrm{C}_{3}-\mathrm{C}_{8}, \mathrm{C}_{4}-\mathrm{C}_{5}, \mathrm{C}_{5}-\mathrm{C}_{6}$, and $\mathrm{C}_{6}-\mathrm{C}_{9}$ are in line with $1.400 \AA$ values. Bond distances of $\mathrm{C}_{9}-\mathrm{C}_{10}$, $\mathrm{C}_{9}-\mathrm{C}_{14}, \mathrm{C}_{10}-\mathrm{C}_{11}, \mathrm{C}_{11}-\mathrm{C}_{12}, \mathrm{C}_{12}-\mathrm{C}_{13}, \mathrm{C}_{13}-\mathrm{C}_{14}, \mathrm{C}_{15}-\mathrm{C}_{16}$, $\mathrm{C}_{15}-\mathrm{C}_{20}, \mathrm{C}_{16}-\mathrm{C}_{17}, \mathrm{C}_{17}-\mathrm{C}_{18}, \mathrm{C}_{18}-\mathrm{C}_{19}$ are having a mean value of $1.39 \AA$ with few exceptions. Almost all $\mathrm{C}-\mathrm{H}$ bond lengths calculated nearly equal to $1.00 \AA$. $\mathrm{N}_{1}-\mathrm{H}_{21}$ bond length is also nearly equal to $1.00 \AA$. Calculated values of $\mathrm{C}_{3}-\mathrm{C}_{4}-\mathrm{O}_{7}$ and $\mathrm{C}_{5}-\mathrm{C}_{4}-\mathrm{O}_{7}$ are $122.6^{\circ}$ and $121.2^{\circ}$, respectively. These are larger bond angle which may be due to electron density in oxygen atoms. $\mathrm{C}-\mathrm{C}-\mathrm{H}$ bond angles are approximately equal to $120^{\circ}$ (phenyl rings). Other than phenyl rings it is nearly equal to $109^{\circ}$. $\mathrm{C}-\mathrm{C}-\mathrm{C}$ angles vary from $109^{\circ}$ to $120^{\circ} . \mathrm{H}-\mathrm{C}-\mathrm{H}$ and $\mathrm{N}-\mathrm{C}-\mathrm{H}$ angles are nearly equal to $108^{\circ} . \mathrm{N}-\mathrm{C}-\mathrm{C}$ angles calculated at both HF and B3LYP methods are nearly equal to $111^{\circ}$. The only $\mathrm{C}_{2}-\mathrm{N}_{1}-\mathrm{C}_{6}$ bond angle is $118^{\circ}$. The dihedral angles


Fig. 1 - Optimized molecular structure of 3-methyl-2, 6-diphenylpiperidin-4-one(MDPO)
between piperidine and phenyl rings are given in Table 1. A few torsional angles of the title compound MDPO are also given in Table 1.

### 4.2 Vibrational assignments

The title molecule MDPO consists of 39 atoms and hence it has 111 normal modes of vibrations. According to classical mechanics, the molecule has 111 normal modes of vibration. For a proper understanding of the IR and Raman spectra of polyatomic molecules typically with modes of vibration exceeding beyond 50, DFT method gives
the more accurate prediction other than calculation methods ${ }^{36}$. The fundamental vibrational wavenumbers of MDPO calculated by DFT (B3LYP/6-311++G(d,p) and HF/6-311++G(d,p) given in Table 2. The calculated vibrational wavenumbers, IR intensities, Raman scattering activities and Raman intensities are compared with experimental FT-IR and FT-Raman frequencies as listed in Table 2. Theoretical FT-IR and FT-Raman spectra of MDPO are shown in Figs 2 and 3. The experimental FT-IR and FT-Raman spectra of MDPO are shown in Figs 4 and 5.

Table 2 - Comparison of the experimental (FT-IR, FT-Raman wavenumbers $\left(\mathrm{cm}^{-1}\right)$ ) and theoretical wavenumbers $\left(\mathrm{cm}^{-1}\right)$, infrared intensities ( $\mathrm{I}^{\mathrm{R}}$ ), Raman scattering activities ( $\mathrm{S}^{\mathrm{Ra}}$ ) and Raman intensities $\left(\mathrm{I}^{\mathrm{RA}}\right.$ ) of MDPO calculated by HF/6-311++G(d,p) and B3LYP/6-31++G(d,p) methods

| Experimental frequency $\left(\mathrm{cm}^{-1}\right)$ |  | Calculated frequency ( $\mathrm{cm}^{-1}$ ) |  |  |  |  |  |  |  | Vibrational assignments |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | HF/6-311++G(d,p) |  |  |  | B3LYP/6-31++G(d,p) |  |  |  |  |
| FTIR | FT-Raman | Unscaled | $\mathrm{I}^{\text {IR }}$ | $S^{\text {RA }}$ | $\mathrm{I}^{\text {RA }}$ | Unscaled | $\mathrm{I}^{\text {IR }}$ | $S^{\text {RA }}$ | $\mathrm{I}^{\text {RA }}$ |  |
|  |  | -68 | 2.96 | 0.84 | -97.97 | -102 | 2.96 | 0.59 | -46.78 | Ring t |
|  | 94 | 96 | 3.98 | 0.33 | 25.52 | -85 | 5.22 | 1.50 | -142.75 | Ring $\omega$ |
|  |  | 111 | 1.60 | 2.87 | 192.60 | 74 | 0.36 | 1.89 | 191.67 | Butterfly |
|  |  | 129 | 0.14 | 2.25 | 128.78 | 98 | 0.28 | 3.06 | 233.31 | Ring $\omega$ |
|  |  | 136 | 0.33 | 2.42 | 130.83 | 101 | 0.20 | 3.20 | 236.85 | C-N $\omega$ |
|  | 190 | 175 | 0.16 | 3.61 | 149.31 | 136 | 0.17 | 3.96 | 214.45 | Ring t |
|  | 225 | 228 | 0.62 | 4.94 | 153.15 | 189 | 0.09 | 4.32 | 164.77 | Ring $\omega$ |
|  | 248 | 260 | 1.70 | 1.58 | 42.51 | 221 | 3.09 | 2.33 | 75.01 | Ring $\omega$ |
|  | 275 | 281 | 1.32 | 0.96 | 23.74 | 253 | 2.35 | 0.35 | 9.59 | Ring $\beta$ |
|  | 294 | 302 | 0.24 | 0.95 | 21.53 | 273 | 0.37 | 1.26 | 31.93 | Ring $\omega$ |
|  |  | 329 | 0.48 | 1.73 | 35.66 | 290 | 3.92 | 2.62 | 62.29 | $\mathrm{C}-\mathrm{C} \omega$ |
|  |  | 336 | 5.59 | 1.79 | 36.02 | 298 | 0.15 | 1.19 | 27.52 | $\mathrm{C}-\mathrm{C} \omega$ |
|  |  | 373 | 1.30 | 4.65 | 82.74 | 340 | 1.21 | 4.88 | 96.68 | Ring $\beta$ |
|  |  | 397 | 2.97 | 0.22 | 3.70 | 356 | 3.65 | 1.15 | 21.61 | Ring $\omega$ |
| 424 |  | 437 | 2.75 | 1.44 | 21.30 | 390 | 3.10 | 3.81 | 64.35 | $\mathrm{C}-\mathrm{H} \omega$ |
| 478 |  | 507 | 2.83 | 0.50 | 6.18 | 454 | 0.22 | 0.08 | 1.07 | $\mathrm{C}-\mathrm{H} \omega$ |
| 525 | $531$ | 514 | 0.89 | 0.15 | 1.87 | 464 | 3.73 | 0.49 | 6.74 | $\mathrm{CH}_{3}$ twis |
|  | 553 | 554 | 4.60 | 0.30 | 3.36 | 470 | 1.44 | 0.39 | 5.36 | $\mathrm{CH}_{3}$ twis |
|  |  | 570 | 0.52 | 0.25 | 2.66 | 501 | 6.27 | 1.23 | 15.33 | $\mathrm{C}-\mathrm{H} \omega$ |
| 598 |  | 597 | 14.38 | 1.28 | 12.86 | 526 | 10.73 | 1.90 | 22.44 | $\mathrm{C}-\mathrm{N} \beta$ |
|  | 619 | 619 | 10.96 | 1.74 | 16.67 | 553 | 5.97 | 1.16 | 12.88 | $\mathrm{C}-\mathrm{H} \omega$ |
|  |  | 620 | 0.77 | 2.46 | 23.60 | 566 | 9.10 | 1.80 | 19.30 | Ring $\omega$ |
|  | 642 | 629 | 10.92 | 1.26 | 11.89 | 576 | 1.56 | 2.48 | 26.09 | Ring $\beta$ |
|  | 669 | 2.69 | 4.20 | 36.51 | 627 | 4.18 | 4.59 | 43.32 | $\mathrm{C}-\mathrm{C} \beta$ |  |
| 675 | 676 | 673 | 1.34 | 7.30 | 62.87 | 629 | 0.19 | 2.48 | 23.26 | $\mathrm{C}-\mathrm{H} \omega$ |
|  |  | 690 | 2.05 | 2.69 | 22.41 | 632 | 0.62 | 4.79 | 44.79 | Ring $\beta$ |
| 694 |  | 699 | 3.11 | 4.86 | 39.80 | 653 | 4.83 | 6.25 | 56.08 | Ring $\beta$ |
|  | 752 | 733 | 0.74 | 2.55 | 19.60 | 678 | 3.17 | 4.08 | 34.80 | $\mathrm{C}=\mathrm{O} \omega$ |
| 791 | 793 | 787 | 5.10 | 7.67 | 53.60 | 729 | 13.55 | 4.25 | 32.89 | $\mathrm{C}-\mathrm{C} \omega$ |
|  |  | 825 | 13.94 | 4.19 | 27.44 | 750 | 25.21 | 2.73 | 20.38 | $\mathrm{C}-\mathrm{H} \omega$ |
| 837 |  | 847 | 11.32 | 1.86 | 11.74 | 768 | 16.63 | 1.10 | 7.95 | $\mathrm{C}-\mathrm{C} \omega$ |
|  | 871 | 866 | 22.14 | 29.71 | 181.78 | 799 | 41.88 | 5.46 | 37.38 | $\mathrm{C}-\mathrm{H} \omega$ |
|  | 882 | 2.41 | 23.99 | 143.10 | 820 | 38.72 | 1.17 | 7.73 | C-H $\omega$ |  |
| 922 | 932 | 930 | 78.99 | 1.01 | 5.61 | 830 | 36.37 | 9.12 | $59.24$ | $\mathrm{C}-\mathrm{H} \omega$ |
|  |  | 938 | 68.99 | 0.72 | 3.95 | 834 | 1.41 | 45.23 | 291.70 | $\mathrm{C}-\mathrm{H} \omega$ |
| 961 | 960 | 959 | 18.66 | 19.59 | 103.66 | 893 | 58.22 | 6.01 | 35.24 | $\mathrm{N}-\mathrm{H} \omega$ |
|  |  | 993 | 0.44 | 2.48 | 12.47 | 907 | 0.85 | 3.81 | 21.87 | $\mathrm{C}-\mathrm{H} \omega$ |

Table 2 - Comparison of the experimental (FT-IR, FT-Raman wavenumbers $\left(\mathrm{cm}^{-1}\right)$ ) and theoretical wavenumbers ( $\mathrm{cm}^{-1}$ ), infrared intensities $\left(I^{\mathbb{R}}\right)$, Raman scattering activities ( $\mathrm{S}^{\mathrm{Ra}}$ ) and Raman intensities $\left(\mathrm{I}^{\mathrm{RA}}\right)$ of MDPO calculated by HF/6-311++G(d,p) and B3LYP/6-31++G(d,p) methods - Contd


Table 2 - Comparison of the experimental (FT-IR, FT-Raman wavenumbers $\left(\mathrm{cm}^{-1}\right)$ ) and theoretical wavenumbers ( $\mathrm{cm}^{-1}$ ), infrared intensities $\left(\mathrm{I}^{\mathrm{IR}}\right)$, Raman scattering activities $\left(\mathrm{S}^{\mathrm{Ra}}\right)$ and Raman intensities $\left(\mathrm{I}^{\mathrm{RA}}\right)$ of MDPO calculated by HF/6-311++G(d,p) and B3LYP/6-31++G(d,p) methods - Contd

| Experimental frequency $\left(\mathrm{cm}^{-1}\right)$ |  | Calculated frequency ( $\mathrm{cm}^{-1}$ ) |  |  |  |  |  |  |  | Vibrational assignments |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | HF/6-311++G(d,p) |  |  |  | B3LYP/6-31++G(d,p) |  |  |  |  |
| FTIR | FT-Raman | Unscaled | $\mathrm{I}^{\text {IR }}$ | $S^{R A}$ | $\mathrm{I}^{\text {RA }}$ | Unscaled | $\mathrm{I}^{\mathrm{IR}}$ | $S^{\text {RA }}$ | $\mathrm{I}^{\text {RA }}$ |  |
|  |  | 1714 | 16.78 | 25.61 | 52.07 | 1591 | 5.55 | 16.44 | 38.37 | $\mathrm{C}-\mathrm{C} v$ |
| 1886 |  | 1872 | 295.52 | 17.84 | 30.56 | 1811 | 16.34 | 2.35 | 4.32 | $\mathrm{H} \cdots \mathrm{H} v$ |
| 1952 |  | 1958 | 15.00 | 2.28 | 3.57 | 1853 | 226.08 | 16.91 | 29.59 | $\mathrm{C}=\mathrm{O} v$ |
| 2928 | 2930 | 2930 | 10.50 | 389.90 | 232.75 | 2813 | 8.78 | 1182.30 | 790.01 | $\mathrm{C}-\mathrm{H} v$-pyridine |
|  |  | 2933 | 24.48 | 109.02 | 64.89 | 2883 | 24.33 | 135.65 | 84.72 | C-H sym $v$-methyl |
|  |  | 2955 | 2.22 | 177.56 | 103.49 | 2889 | 8.82 | 33.97 | 21.09 | $\mathrm{C}-\mathrm{H}$ sym $v$ - $\left(\mathrm{CH}_{2}\right)$ |
|  |  | 2957 | 35.49 | 78.05 | 45.44 | 2904 | 20.78 | 114.07 | 69.87 | $\mathrm{C}-\mathrm{H} v$-pyridine |
|  |  | 2959 | 23.97 | 245.76 | 142.68 | 2907 | 12.70 | 46.96 | 28.69 | $\mathrm{C}-\mathrm{H} v$-pyridine |
| 2974 | 2975 | 2986 | 35.46 | 66.86 | 37.83 | 2948 | 2.52 | 97.03 | 56.94 | $\mathrm{C}-\mathrm{H}$ asym v-( $\mathrm{CH}_{2}$ ) |
|  | 2996 | 16.51 | 64.16 | 35.99 | 2949 | 27.77 | 26.77 | 15.70 |  | $\mathrm{C}-\mathrm{H}$ asymv-( $\mathrm{CH}_{3}$ ) |
| 3028 | 3044 | 2998 | 34.50 | 54.34 | 30.39 | 2959 | 20.30 | 59.93 | 34.80 | $\mathrm{C}-\mathrm{H}$ asym $v$ - $\left(\mathrm{CH}_{3}\right)$ |
| 3063 | 3059 | 3100 | 2.43 | 32.42 | 16.46 | 3041 | 10.85 | 18.06 | 9.70 | $\mathrm{C}-\mathrm{H}$ asymv-phenyl |
|  |  | 3101 | 1.59 | 34.37 | 17.43 | 3054 | 1.96 | 36.42 | 19.32 | $\mathrm{C}-\mathrm{H}$ asym v-phenyl |
|  |  | 3109 | 2.75 | 141.88 | 71.41 | 3056 | 0.78 | 54.20 | 28.69 | $\mathrm{C}-\mathrm{H}$ asym v-phenyl |
|  |  | 3110 | 13.18 | 85.49 | 42.99 | 3061 | 1.97 | 131.94 | 69.51 | $\mathrm{C}-\mathrm{H}$ asym v-phenyl |
|  |  | 3118 | 22.59 | 39.67 | 19.80 | 3064 | 3.35 | 117.03 | 61.46 | $\mathrm{C}-\mathrm{H}$ asym v-phenyl |
|  |  | 3118 | 13.93 | 72.79 | 36.29 | 3069 | 21.47 | 63.10 | 32.99 | $\mathrm{C}-\mathrm{H}$ asym v-phenyl |
|  |  | 3125 | 16.98 | 14.85 | 7.36 | 3073 | 25.66 | 58.05 | 30.24 | $\mathrm{C}-\mathrm{H}$ asym v-phenyl |
|  |  | 3126 | 23.62 | 15.58 | 7.71 | 3076 | 21.85 | 21.07 | 10.94 | $\mathrm{C}-\mathrm{H}$ asym $v$-phenyl |
|  |  | 3133 | 24.64 | 313.79 | 514.35 | 3082 | 22.95 | 337.59 | 174.31 | $\mathrm{C}-\mathrm{H}$ sym v-phenyl |
| 3167 |  | 3134 | 13.21 | 330.91 | 162.62 | 3083 | 14.11 | 404.30 | 208.56 | $\mathrm{C}-\mathrm{H}$ sym $v$-phenyl |
| 3522 | 3298 | 3530 | 4.19 | 59.29 | 19.92 | 3492 | 2.16 | 77.32 | 26.94 | $\mathrm{N}-\mathrm{H} v$ |

$\omega$, out-of-plane bending; $\beta$, in-plane-bending; t,torsion; twis, twisting; rock, rocking; $v$, stretching; $\delta$ rock, out-of-plane rocking; $\alpha$ rock, in-plane-rocking; wag-wagging; scis, scissoring; ip-def, in-plane deformation; sym $v$, symmetric stretching; asym $v$, asymmetric stretching


Fig. 2 - Theoretical IR intensity spectrum of MDPO

### 4.2.1 $\mathrm{N}-\mathrm{H}$ vibrations

The $\mathrm{N}-\mathrm{H}$ stretching vibration ${ }^{17,18}$ appears strongly and broadly in the region $3500-3300 \mathrm{~cm}^{-1}$. Erdogdu et al ${ }^{19}$. assigned $\mathrm{N}-\mathrm{H}$ stretching mode in the region $3500-3300 \mathrm{~cm}^{-1}$. In this study, the peak was observed


Fig. 3 - Theoretical Raman Activity spectrum of MDPO


Fig. 4 - FT-IR Experimental spectrum of MDPO


Fig. 5 - FT-Raman Experimental spectrum of MDPO
as medium and narrow band in FT-IR, but weak and narrow bands in FT-Raman, where the peaks are attributed to $3387 \mathrm{~cm}^{-1}$ and $3298 \mathrm{~cm}^{-1}$ for FT-IR and FT-Raman, respectively. The corresponding theoretical peak for $\mathrm{N}-\mathrm{H}$ stretching mode is about $3492 \mathrm{~cm}^{-1}$ in B3LYP/6-311++G (d, p) basis set and $3530 \mathrm{~cm}^{-1}$ in HF/6-311++G ( $\mathrm{d}, \mathrm{p}$ ) basis set which shows positive deviation from the experimental value. The $\mathrm{N}-\mathrm{H}$ stretching fundamental of piperidine was observed in the vapour phase ${ }^{20}$ at $3364 \mathrm{~cm}^{-1}$. The position of the methyl group in the piperidine ring influences the $\mathrm{N}-\mathrm{H}$ stretching wavenumber. Out-ofplane bending modes $(\mathrm{N}-\mathrm{H})$ is calculated at $892 \mathrm{~cm}^{-1}$. This vibration is in agreement with the observed FT-IR ( $921 \mathrm{~cm}^{-1}$ ) and FTRaman ( $871 \mathrm{~cm}^{-1}$ ) bands.

### 4.2.2 $\mathrm{CH}_{3}$ and $\mathrm{CH}_{2}$ group vibrations

Methyl groups are, generally, referred to as electron donating substituents in the aromatic ring system ${ }^{21}$. In acetates, the asymmetric vibrations of the methyl group are expected to occur in the region 2940$3040 \mathrm{~cm}^{-1}$ and symmetric vibrations are in the region $2910-2930 \mathrm{~cm}^{-1}$, and usually the bands are weak ${ }^{22}$. Aromatic acetyl substituent absorbs in a narrow range $3000-3020 \mathrm{~cm}^{-1}$ and the absorption sometimes coincides with a $\mathrm{C}-\mathrm{H}$ stretching mode of the ring. The title molecule possesses methyl $\left(\mathrm{CH}_{3}\right)$ and methylene $\left(\mathrm{CH}_{2}\right)$ groups. For the assignments of $\mathrm{CH}_{3}$ group frequencies, basically, nine fundamentals can be associated to $\mathrm{CH}_{3}$ group namely, $\mathrm{CH}_{3} \mathrm{sym}$, symmetric stretch, $\mathrm{CH}_{3}$ asym, asymmetric stretch, $\mathrm{CH}_{3}$ ipscis, in-plane scissoring. $\mathrm{CH}_{3}$ op scis, out-of-plane scissoring, $\mathrm{CH}_{3}$ ip bend, in-plane bending, $\mathrm{CH}_{3}$ op bend, out-of-plane bending, $\mathrm{CH}_{3}$ ip twist, in-plane twisting, $\mathrm{CH}_{3}$ op twist, out-of plane twisting and $\mathrm{CH}_{3}$ torsion modes. Methyl in-plane deformations occur theoretically at 1518 and $1450 \mathrm{~cm}^{-1}$ wavenumbers and methyl in-plane bending at $1514 \mathrm{~cm}^{-1}$. These two vibrations have experimental support at $1492 \mathrm{~cm}^{-1}$ in FT-IR and at $1449 \mathrm{~cm}^{-1}$ in FT-Raman spectra. Methyl out-of-bending vibration is predicted at 1122 and $1140 \mathrm{~cm}^{-1}$. The corresponding sharp peaks were found experimentally at $1141 \mathrm{~cm}^{-1}$ in FT-IR and at $1152 \mathrm{~cm}^{-1}$ in FT-Raman spectra. The methyl twisting predicted theoretically at 464 and $470 \mathrm{~cm}^{-1}$ has a sharp peak at $478 \mathrm{~cm}^{-1}$ in FT-IR spectrum.

For the assignments of $\mathrm{CH}_{2}$ group frequencies, basically six fundamentals can be associated to each $\mathrm{CH}_{2}$ group namely, $\mathrm{CH}_{2}$ sym, symmetric stretch,
$\mathrm{CH}_{2}$ asym, asymmetric stretch, $\mathrm{CH}_{2}$ scis, scissoring and $\mathrm{CH}_{2}$ rock, rocking modes which belong to polarized in-plane vibrations. In addition to that $\mathrm{CH}_{2}$ wag, wagging and $\mathrm{CH}_{2}$ twist, twisting modes of $\mathrm{CH}_{2}$ group would be expected to be depolarized for out-of-plane bending vibrations. The $\mathrm{C}-\mathrm{H}$ stretching vibrations of the methylene group are at lower frequencies than those of the aromatic $\mathrm{C}-\mathrm{H}$ ring stretching. The asymmetric $\mathrm{CH}_{2}$ stretching vibration is, generally, observed in the region $3000-2900 \mathrm{~cm}^{-1}$, while the $\mathrm{CH}_{2}$ symmetric stretching will appear between 2900 and $2800 \mathrm{~cm}^{-1}$ (Ref. 23). In the present study, it is evident for $\mathrm{C}-\mathrm{H}$ symmetric stretching of mehthylene group at $2889 \mathrm{~cm}^{-1}$ and for $\mathrm{C}-\mathrm{H}$ asymmetric stretching of methylene group at $2948 \mathrm{~cm}^{-1}$. The $\mathrm{CH}_{2}$ symmetric stretching vibrations are observed at $2889 \mathrm{~cm}^{-1}$ in FT-IR and at $2903 \mathrm{~cm}^{-1}$ in FT-Raman spectra. The $\mathrm{CH}_{2}$ asymmetric stretching vibrations are observed at $2927 \mathrm{~cm}^{-1}$ in FT-IR and at $2930 \mathrm{~cm}^{-1}$ in FT-Raman spectra. In the present assignment, the $\mathrm{CH}_{2}$ bending modes follow in decreasing wavenumber with the general order $\mathrm{CH}_{2}$ scissoring $>\mathrm{CH}_{2}$ wagging $>\mathrm{CH}_{2}$ twist> $\mathrm{CH}_{2}$ rock. The computed wavenumber of $1504 \mathrm{~cm}^{-1}$ for $\mathrm{CH}_{2}$ scissoring is in line with peak at $1492 \mathrm{~cm}^{-1}$ in FTIR spectrum. For $\mathrm{CH}_{2}$ wagging, calculated value of $1340 \mathrm{~cm}^{-1}$ is in line with strong peak at $1338 \mathrm{~cm}^{-1}$ in FT-IR and medium peak at $1353 \mathrm{~cm}^{-1}$ in FT-Raman spectra. $\mathrm{CH}_{2}$ twisting calculated at $1257 \mathrm{~cm}^{-1}$ is in line with weak bands at $1273 \mathrm{~cm}^{-1}$ in FT-IR and at $1232 \mathrm{~cm}^{-1}$ in FT-Raman spectra. $\mathrm{CH}_{2}$ rocking calculated at $1004 \mathrm{~cm}^{-1}$ is in line with peak at $1001 \mathrm{~cm}^{-1}$ in FT-Raman spectra.

### 4.2.3 $C=O$ vibrations

Stretching vibration of carbonyl group $\mathrm{C}=\mathrm{O}$ can be observed as a very strong band in both FT-IR and FT-Raman spectra ${ }^{24}$ at $1665 \mathrm{~cm}^{-1}$. The carbonyl stretching $\mathrm{C}=\mathrm{O}$ vibration ${ }^{22}$ is expected to occur in the region 1715-1680 $\mathrm{cm}^{-1}$. The deviation of the calculated wavenumbers for this mode can be attributed to the underestimation of the large degree of $\pi$-electron delocalization due to conjugation of the molecule. In the present paper, we have observed stretching vibrations of $\mathrm{C}=\mathrm{O}$ at 1338. 1701 and $1886 \mathrm{~cm}^{-1}$ in FT-IR. with $1701 \mathrm{~cm}^{-1}$ being very strong band and at 1353 and $1701 \mathrm{~cm}^{-1}$ in FT-Raman, the latter being strong band. The computed frequencies are 1386 and $1853 \mathrm{~cm}^{-1}$ for $\mathrm{C}=\mathrm{O}$ stretching vibrations. $\mathrm{C}=\mathrm{O}$ out-of-plane bending is computed at $678 \mathrm{~cm}^{-1}$. The experimental peaks at 675
and $694 \mathrm{~cm}^{-1}$ in FT-IR spectrum and at $676 \mathrm{~cm}^{-1}$ in FT-Raman spectrum are in line with the computed value.

### 4.2.4 C-N vibrations

The identification of $\mathrm{C}-\mathrm{N}$ vibration is a very difficult task, since mixing of several bands are possible in this region. In the gas phase spectrum of the piperidine molecule Vedal et $a l^{20}$. observed the $\mathrm{C}-\mathrm{N}$ stretching at 1147 and $1313 \mathrm{~cm}^{-1}$ and in solid state piperidine molecule Gulluoglu et al ${ }^{25}$. observed the $\mathrm{C}-\mathrm{N}$ stretching at 1135 and $1317 \mathrm{~cm}^{-1}$. The theoretical wavenumbers for $\mathrm{C}-\mathrm{N}$ stretching vibrations in this title molecule are 1048 and $1097 \mathrm{~cm}^{-1}$. The $\mathrm{C}-\mathrm{N}$ in-plane and out-of plane bending vibrations are at 100 and $526 \mathrm{~cm}^{-1}$. respectively. The experimental peak values that are in line with theoretical wavenumbers are (FT-IR: 1029 and $1099 \mathrm{~cm}^{-1}$, FT-Raman: 1034 and $1086 \mathrm{~cm}^{-1}$ ) for $\mathrm{C}-\mathrm{N}$ stretching vibrations. C-N in-plane bending vibrations calculated at $526 \mathrm{~cm}^{-1}$ has experimental peaks at $530 \mathrm{~cm}^{-1}$ in FT-Raman and at $524 \mathrm{~cm}^{-1}$ in FT-IR spectra. C-N out-of-plane bending vibration predicted at $100 \mathrm{~cm}^{-1}$ has experimental peak at $94 \mathrm{~cm}^{-1}$ in FT-Raman spectrum only. The C-N stretching vibration ${ }^{22}$ normally appears around $1300 \mathrm{~cm}^{-1}$. In the present work, the $\mathrm{C}-\mathrm{N}$ stretching frequencies are reasonably lowered.

### 4.2.5 C-C vibrations

The carbon-carbon stretching modes of the pyridine are expected in the range $1650-1100 \mathrm{~cm}^{-1}$ which are not significantly influenced by the nature of the substituents ${ }^{26}$. The $\mathrm{C}-\mathrm{C}$ stretching vibrations of phenyl ring and methylene are calculated in the range $1591-1068 \mathrm{~cm}^{-1}$. These vibrations are in line with experimental values (1072, 1099, 1141, 1222, 1273 and $1597 \mathrm{~cm}^{-1}$ in FT-IR and 1086, 1152, 1175, 1207, 1232 and $1585 \mathrm{~cm}^{-1}$ in FT-Raman). C-C out-of-plane bending vibrations are theoretically calculated at 290, 297, 729 and $768 \mathrm{~cm}^{-1}$ and C-C in-plane bending vibration is calculated at $626 \mathrm{~cm}^{-1}$ which are found to be in agreement in both IR and Raman experimental spectra.

### 4.2.6 $\mathbf{C}-\boldsymbol{H}$ vibrations

The $\mathrm{C}-\mathrm{H}$ stretching modes of the ring and methyl group were observed at $2730 \mathrm{~cm}^{-1}, 2800 \mathrm{~cm}^{-1}$, $2868 \mathrm{~cm}^{-1}$ and $2920 \mathrm{~cm}^{-1}$ for 3-methylpiperidine ${ }^{27}$. The $\mathrm{C}-\mathrm{H}$ stretching modes were predicted in the
range $2813-3083 \mathrm{~cm}^{-1}$. One can also expect $\mathrm{C}-\mathrm{H}$ stretching vibrations for the title molecule as a very strong band in FTRaman spectrum at 2811, 2903, 2930, 2975, 3043 and $3058 \mathrm{~cm}^{-1}$ and strong FT-IR bands at 2808, 2862, 2889, 2927, 2974, 3028 and $3062 \mathrm{~cm}^{-1}$. are assigned to $\mathrm{C}-\mathrm{H}$ stretching vibration. The theoretically computed wavenumbers from 2813 to $3083 \mathrm{~cm}^{-1}$ show good agreement with the recorded spectra. Vedal et al ${ }^{20}$. assigned the $\mathrm{C}-\mathrm{H}$ stretching vibration in piperidine molecule at $2925 \mathrm{~cm}^{-1}$ in gas phase spectrum, Gulluoglu et al ${ }^{25}$. assigned the $\mathrm{C}-\mathrm{H}$ stretching vibration in piperidine molecule by B3LYP/6-31G (d) method at $2911 \mathrm{~cm}^{-1}$. The theoretical results show that the computed value by B3LYP/6-311++G( $\mathrm{d}, \mathrm{p}$ ) method is in good agreement with the literature value. The $\mathrm{C}-\mathrm{H}$ in-plane bending modes of vibrations are assigned for the wavenumbers in the range $1160-1572 \mathrm{~cm}^{-1}$. The lower experimental peaks in support to this range are $1141,1338,1446$ and $1492 \mathrm{~cm}^{-1}$ in FT-IR and 1152, 1175, 1353 and $1449 \mathrm{~cm}^{-1}$ in FT-Raman spectra. The C-H out-ofplane bending modes of vibration are assigned for the wavenumbers in the range $390-1034 \mathrm{~cm}^{-1}$. The extreme lower experimental peaks in support to this range are $478,524,597,694,752,837,921$ and $960 \mathrm{~cm}^{-1}$ in FT-IR and 553, 619, 641,792, 932, 960, $1001 \mathrm{~cm}^{-1}$ in FT-Raman spectra.

### 4.2.7 Ring vibrations

These modes are not pure but they contribute drastically from other vibrations and are substituentsensitive. In the title molecule, ring in-plane and out-of-plane bending modes are affected to a great extent by the substituents and produce bands below $660 \mathrm{~cm}^{-1}$ and few bands near $1000 \mathrm{~cm}^{-1}$. The calculated theoretical wavenumbers of ring torsion, ring in-plane bending, ring out-of plane bending, ring breathing and butterfly vibrational modes are discussed here. The only ring torsion effect is observed at $136 \mathrm{~cm}^{-1}$. Ring in-plane bending vibrations are assigned at $252,339,575,631,652$, 978, 992 and $1012 \mathrm{~cm}^{-1}$. Ring out-of-plane bending vibrations are assigned at $98,188,273,355$ and $566 \mathrm{~cm}^{-1}$. A peculiar ring vibration called butterfly vibration mode observed at $74 \mathrm{~cm}^{-1}$ is because of both the phenyl rings approach and recede alternatively. The peaks for these modes are not observed in FT-IR spectrum since these modes are possible to appear only in far IR spectrum. The weak intensity bands present at 189 and $275 \mathrm{~cm}^{-1}$ in FT-Raman spectrum
are assigned to ring out-of-plane bending. The medium intensity band $641 \mathrm{~cm}^{-1}$ and a strong band at $1001 \mathrm{~cm}^{-1}$ in FT-Raman spectrum are assigned to ring in-plane bending. The theoretical wavenumbers corresponding to ring vibrations are found to have agood correlation with the available experimental observations.

## 5 UV Analysis

The lowest singlet $\rightarrow$ singlet spin allowed excited states need to be accounted to investigate the electronic transition ${ }^{40}$. The absorption wavelength, excitation energies and oscillator strength for the title molecule in the solvents methanol, benzene and water are computed using TD/HF-6311++G(d,p) method. The solvent effects on the absorption wavelengths and excitation energies are examined by the Polarizable continuum Model using TD/HF-6311++G(d,p) method. The three absorption peaks of the title molecule have a mean oscillator strength (say $\sim 0.016 \mathrm{au}$ ). The simulated theoretical UV-spectrum of MDPO are shown in Figs 6-8. In the electronic spectrum, the strong intensity peaks at the maximum absorption wavelength of ( 223.74 nm ) in methanol), ( 224.43 nm in benzene) and ( 223.71 nm in water) are caused by $n \rightarrow \pi^{*}$ transitions, while the smaller intensity bands calculated near 242 nm in water and methanol and at 246 in benzene phases of the title molecule are forbidden and therefore, the oscillator strengths of these phases nearly equal to zero. The calculated spectra agree with the experimental UV spectra of MDPO with methanol, benzene and water solvents as shown in Figs 6a, 7a and 8a, respectively. UV analysis of 3-methyl-2,6-diphenylpiperidin-4-one is shown in Table 3 with theoretical absorption wavelength $\lambda(\mathrm{nm})$, excitation energies $E(\mathrm{eV})$ and


Fig. 6 - Theoretical UV spectrum - methanol solvent in MDPO


Fig. 6(a)-Experimental UV spectrum - methanol solvent in MDPO


Fig. 7 - Theoretical UV spectrum - benzene solvent in MDPO


Fig. 7(a) - Experimental UV spectrum - methanol solvent in MDPO


Fig. 8 - Theoretical UV spectrum - water solvent in MDPO
oscillator strengths (f) using TD-DFT/B3LYP/6$311++G(d, p)$ method in solvents such as methanol, benzene and water.

## 6 Mulliken Charge Distribution

The Mulliken charge is directly related to the vibrational properties of the molecule, and quantifies how the electronic structure changes under atomic displacement; it is therefore, related directly to the chemical bonds present in the molecule. It affects dipole moment, polarizability, electronic structure and more properties of molecular systems. The Mulliken and natural charge distribution of the molecule are calculated for MDPO on HF and B3LYP levels with $6-311++G(d, p)$ basis set in HF and B3LYP methods. The calculated values of the charges of title molecule are given in Table 4. Distribution of positive and negative charges is vital in increasing or decreasing of bond length between atoms. The charge changes with basis set presumably occurs due to polarization. Considering the two methods of basis set used in the atomic charge calculation, the oxygen atoms exhibit a negative charge, which are donor atoms. The charges of $\mathrm{N}_{1}, \mathrm{C}_{3}, \mathrm{C}_{9}$ and $\mathrm{C}_{15}$ are positive in HF and B3LYP methods with $6-311++G(d, p)$ basis set. In the case of $\mathrm{C}_{2}$ and $\mathrm{C}_{6}$, the charges are positive in HF method with $6-311++G(d, p)$ basis set and negative in B3LYP method with $6-311++G(d, p)$ set, but in the case of $\mathrm{C}_{20}$, the charges are negative in HF method with


Fig. 8(a) - Experimental UV spectrum - methanol solvent in MDPO
$6-311++G(d, p)$ basis set and positive in B3LYP method with $6-311++G(d, p)$ basis set. The rest of the carbon atoms have negative charge. Moreover, positive charge distribution is observed in the remaining 19 hydrogen atoms $\left(\mathrm{H}_{21}\right.$ to $\left.\mathrm{H}_{39}\right)$. Oxygen $\mathrm{O}_{7}$ is negative in both methods with the largest value of

Table 4 - Mulliken atomic charges

| Atom <br> type | HF <br> $6-311++\mathrm{G}(\mathrm{d}, \mathrm{p})$ | B 3 LYP |
| :---: | :---: | :---: |
| $\mathrm{N}_{1}$ | 0.008139 | 0.217646 |
| $\mathrm{C}_{2}$ | 0.114943 | -1.530317 |
| $\mathrm{C}_{3}$ | 0.068334 | 0.417109 |
| $\mathrm{C}_{4}$ | -0.065584 | -0.535547 |
| $\mathrm{C}_{5}$ | -0.901323 | -0.733911 |
| $\mathrm{C}_{6}$ | 0.065610 | -0.640542 |
| $\mathrm{O}_{7}$ | -0.307305 | -0.278934 |
| $\mathrm{C}_{8}$ | -0.614776 | -1.194469 |
| $\mathrm{C}_{9}$ | 0.301647 | 0.134169 |
| $\mathrm{C}_{10}$ | -0.233714 | -0.441500 |
| $\mathrm{C}_{11}$ | -0.438648 | -0.379062 |
| $\mathrm{C}_{12}$ | -0.435560 | -0.314956 |
| $\mathrm{C}_{13}$ | -0.261763 | -0.181896 |
| $\mathrm{C}_{14}$ | -0.077237 | -0.045208 |
| $\mathrm{C}_{15}$ | 0.786042 | 0.988742 |
| $\mathrm{C}_{16}$ | -0.160299 | -0.546005 |
| $\mathrm{C}_{17}$ | -0.257254 | -0.440348 |
| $\mathrm{C}_{18}$ | -0.571342 | -0.335386 |
| $\mathrm{C}_{19}$ | -0.463365 | -0.365023 |
| $\mathrm{C}_{20}$ | -0.371770 | 0.324660 |
| $\mathrm{H}_{21}$ | 0.279487 | 0.382510 |
| $\mathrm{H}_{22}$ | 0.249559 | 0.347794 |
| $\mathrm{H}_{23}$ | 0.169673 | 0.342290 |
| $\mathrm{H}_{24}$ | 0.242977 | 0.351487 |
| $\mathrm{H}_{25}$ | 0.217353 | 0.307416 |
| $\mathrm{H}_{26}$ | 0.176733 | 0.275339 |
| $\mathrm{H}_{27}$ | 0.177649 | 0.272839 |
| $\mathrm{H}_{28}$ | 0.188983 | 0.295927 |
| $\mathrm{H}_{29}$ | 0.136546 | 0.243606 |
| $\mathrm{H}_{30}$ | 0.184972 | 0.310894 |
| $\mathrm{H}_{31}$ | 0.211269 | 0.287764 |
| $\mathrm{H}_{32}$ | 0.187962 | 0.270829 |
| $\mathrm{H}_{33}$ | 0.214887 | 0.288590 |
| $\mathrm{H}_{34}$ | 0.229141 | 0.346076 |
| $\mathrm{H}_{35}$ | 0.181403 | 0.313050 |
| $\mathrm{H}_{36}$ | 0.224594 | 0.298996 |
| $\mathrm{H}_{37}$ | 0.180789 | 0.270631 |
| $\mathrm{H}_{38}$ | 0.223452 | 0.291610 |
| $\mathrm{H}_{39}$ | 0.176567 | 0.383129 |
|  |  |  |

Table 3 - Theoretical electronic absorption spectra (UV) of MDPO (absorption wavelength $\lambda$ (nm), excitation energies $E(\mathrm{eV})$ and oscillator strengths (f)) using TD-DFT/B3LYP/6-311++G(d,p) method

| Excitation states | Methanol |  |  | Benzene |  |  | Water |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\lambda(\mathrm{nm})$ | $\Delta E(\mathrm{eV})$ | $f$ (a.u.) | $\lambda(\mathrm{nm})$ | $\Delta E(\mathrm{eV})$ | $f$ (a.u.) | $\lambda(\mathrm{nm})$ | $\Delta \mathrm{E}(\mathrm{eV})$ | $f$ (a.u.) |
| Excitated state 1 | 242.25 | 5.1180 | 0.0008 | 246.74 | 5.0250 | 0.0008 | 242.00 | 5.1233 | 0.0008 |
| Excitated state 2 | 226.84 | 5.4658 | 0.0155 | 227.84 | 5.4417 | 0.0155 | 226.81 | 5.4664 | 0.0155 |
| Excitated state 3 | 223.74 | 5.5414 | 0.0002 | 224.43 | 5.5245 | 0.0002 | 223.71 | 5.5422 | 0.0002 |

-0.30731 a.u in HF method with $6-311++G(\mathrm{~d}, \mathrm{p})$ basis set. The atomic charges of carbon, nitrogen and oxygen are presented in Table 4.

## 7 Thermodynamic Properties

The values of some thermodynamic parameters such as zero point vibrational energy, thermal energy, specific heat capacity, rotational constants, entropy, and dipole moment of MDPO by DFT/B3LYP with $6-31++G(d, p)$ basis set and HF method with/6$311++G(d, p)$ basis set are listed in Table 5. The global minimum energy(SCF) obtained for structure optimization of MDPO with $6-311++G(d, p)$ basis set is -827 au for DFT/B3LYP. The minimum energy becomes -822 au for HF/6-311G++ ( $\mathrm{d}, \mathrm{p}$ ) basis set. The difference in amount of energy between the methods is ca. 5 au only. The rotational constant values are observed to be the same in both basis sets of HF and B3LYP methods. The variation in zeropoint vibrational energies (ZPVEs) seems to be significant. The biggest value of ZPVE of MDPO is $218.596 \mathrm{kcal} \mathrm{mol}^{-1}$ obtained at $\mathrm{HF} / 6-311++\mathrm{G}(\mathrm{d}, \mathrm{p})$, whereas the smallest value is $206.665 \mathrm{kcal} \mathrm{mol}^{-1}$ obtained at B3LYP/6-311++G(d,p).

Dipole moment reflects the molecular charge distribution and is given as a vector in three
dimensions. Therefore, it can be used as descriptor to depict the charge movement across the molecule. Direction of the dipole moment vector in a molecule depends on the centres of positive and negative charges. Dipole moments are strictly determined for neutral molecules. For charged systems, its value depends on the choice of origin and molecular orientation. As a result of HF and DFT (B3LYP) calculations, the highest dipole moment(4.2137D) was observed for $\mathrm{HF} / 6-311 \mathrm{G}++(\mathrm{d}, \mathrm{p})$, whereas the smallest one(3.6836D) was observed for B3LYP/6$31++G(d, p)$ in MDPO.

## 8 HOMO-LUMO

Molecular orbitals (HOMO and LUMO) and their properties such as energy are very useful for physicists and chemists and are very important parameters for quantum chemistry. This is also used by the frontier electron density for predicting the most reactive position in $\pi$-electron systems and also explains several types of reaction in conjugated system ${ }^{28}$. Both the highest occupied molecular orbital (HOMO) and lowest unoccupied molecular orbital (LUMO) are the main orbitals taking part in chemical stability. The frontier molecular orbitals play an important role in the electric and optic properties, as

Table 5 - Theoretically computed zero point vibrational energy ( $\mathrm{kcal} \mathrm{mol}^{-1}$ ), rotational constants ( GHz ), rotational temperature ( K ), thermal energy ( $\mathrm{kcal} \mathrm{mol}^{-1}$ ), molar capacity at constant volume ( $\mathrm{cal} \mathrm{mol}^{-1} \mathrm{~K}^{-1}$ ) entropies ( $\mathrm{cal} \mathrm{mol}^{-1} \mathrm{~K}^{-1}$ )

| Parameters | HF/6-311++G(d,p) | B3LYP/6-311++G(d,p) |
| :--- | :---: | :---: |
|  |  |  |
| Self-consistent field energy(a.u.) | -822.08672 | -827.30191 |
| Zero-point vibrational energy | 218.596 | 206.665 |
| Rotational temperature | 0.02273 | 0.02273 |
|  | 0.01302 | 0.01302 |
| Rotational constants | 0.00940 | 0.00940 |
|  | 0.47372 | 0.47372 |
| Energy | 0.27129 | 0.27129 |
| Translational | 0.19579 | 0.19579 |
| $\quad$ Rotational | 0.889 |  |
| $\quad$ Vibrational | 0.889 | 0.889 |
| Total | 224.980 | 0.889 |
| Molar capacity at constant volume | 226.757 | 213.562 |
| Translational |  | 215.340 |
| Rotational | 2.981 |  |
| Vibrational | 2.981 | 2.981 |
| Total | 50.464 | 2.981 |
| Entropy | 56.426 | 54.539 |
| Translational |  | 60.501 |
| Rotational | 42.625 | 42.625 |
| Vibrational | 33.812 | 33.812 |
| Total | 35.556 | 38.890 |
| Dipole moment | 111.993 | 115.327 |

well as in UV-Vis spectra and chemical reactions. The analysis of the wave function indicates that the electron absorption corresponds to the transition from the ground to the first excited state and is mainly described by one electron-excitation from the highest occupied molecular orbital (HOMO) to the lowest unoccupied orbital (LUMO). The bioactivity and chemical activity of the molecule depends on eigen value of HOMO, LUMO and energy gap. HOMO as an electron donor represents the ability to donate an electron. LUMO as an electron acceptor represents the ability to obtain an electron. The energy of HOMO is directly related to the ionization potential, and that of LUMO is directly related to electron affinity. The energy difference between the HOMO and LUMO is about 4.9427 eV . The smaller band gap increases the stability of the molecule. The frontier molecular orbitals are shown in Figs 9 and 10. The HOMO and LUMO energy calculated by B3LYP/6$311++G(d, p)$ method in gas phase is given below.

HOMO energy $($ B3LYP $)=-6.1179 \mathrm{eV}$
LUMO energy $(B 3 L Y P)=-1.1752 \mathrm{eV}$
HOMO - LUMO energy gap $(B 3 L Y P)=4.9427 \mathrm{eV}$

## 9 NBO Analysis

### 9.1 Natural Population Analysis

The natural population analysis performed on the electronic structure of title molecule clearly describes the distribution of electrons in various sub-shells of their atomic orbitals. The accumulation of charges on the individual atom and accumulation of electrons in

$\mathrm{HOMO}=-6.1179 \mathrm{eV}$
Fig. 9 - HOMO Plot of MDPO
the core, valence and Rydberg sub-shells of MDPO are presented in Table 6.The most electronegative atoms like $\mathrm{N}_{1}, \mathrm{O} 7$ and $\mathrm{C}_{8}$ have charges -0.69074 , -0.61686 and -0.52510 . respectively. The most electropositive atom is $\mathrm{C}_{4}$ with charge 0.66144 . From the electrostatic point of view, electronegative atoms have a tendency to donate an electron, whereas the electropositive atoms have a tendency to accept an electron. Further, natural population analysis showed that 142 electrons in the title compound are distributed on the sub-shells as follows:

Core: 39.9854 ( $99.9637 \%$ of 40)
Valence: 101.6257 ( $99.6331 \%$ of 102)
Rydberg : 0.38873 ( 0.2738 \% of 142)

### 9.2 Natural Atomic Orbitals

The occupancies and energies of lone pair molecular orbitals (LP) and anti-bonding (BD*) molecular orbitals of the MDPO are predicted at HF/6-311++G level of theory and is presented in Table 7. The variations in occupancies and energies of the title molecule directly give the evidence for the delocalization of charge upon substitution and this leads to the variation of bond lengths.

### 9.3 Natural Bond Orbital Analysis

The interactions result in a loss of occupancy from the localised NBO of the idealized Lewis structure into an empty Non-Lewis orbital. NBO analysis of some pharmaceutical compounds has been performed by many spectroscopists ${ }^{37-39}$. The lone pair-antibonding interaction can be quantitatively described by


Fig. 10 - LUMO Plot of MDPO, $\Delta \mathrm{E}=4.9427 \mathrm{eV}$

Table 6 - Accumulation of natural charges population of electrons in core, valence and Rydberg orbitals of MDPO

| Atom | Charge | Natural Population |  | Total |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
|  |  | Core | Valence | Rydberg |  |
|  |  |  |  |  |  |
| $\mathrm{N}_{1}$ | -0.69074 | 1.99955 | 5.67550 | 0.01569 | 7.69074 |
| $\mathrm{C}_{2}$ | -0.00802 | 1.99919 | 3.98431 | 0.02452 | 6.00802 |
| $\mathrm{C}_{3}$ | -0.30023 | 1.99917 | 4.28683 | 0.01423 | 6.30023 |
| $\mathrm{C}_{4}$ | 0.66144 | 1.99934 | 3.30135 | 0.03787 | 5.33856 |
| $\mathrm{C}_{5}$ | -0.45025 | 1.99927 | 4.43582 | 0.01516 | 6.45025 |
| $\mathrm{C}_{6}$ | -0.05376 | 1.99915 | 4.02929 | 0.02532 | 6.05376 |
| $\mathrm{O}_{7}$ | -0.61686 | 1.99977 | 6.60613 | 0.01096 | 8.61686 |
| $\mathrm{C}_{8}$ | -0.52510 | 1.99947 | 4.51646 | 0.00917 | 6.52510 |
| $\mathrm{C}_{9}$ | -0.03049 | 1.99913 | 4.01252 | 0.01883 | 6.03049 |
| $\mathrm{C}_{10}$ | -0.20370 | 1.99918 | 4.18895 | 0.01557 | 6.20370 |
| $\mathrm{C}_{11}$ | -0.19542 | 1.99928 | 4.17765 | 0.01849 | 6.19542 |
| $\mathrm{C}_{12}$ | -0.21226 | 1.99928 | 4.19456 | 0.01843 | 6.21226 |
| $\mathrm{C}_{13}$ | -0.19087 | 1.99928 | 4.17334 | 0.01825 | 6.19087 |
| $\mathrm{C}_{14}$ | -0.19738 | 1.99918 | 4.18237 | 0.01584 | 6.19738 |
| $\mathrm{C}_{15}$ | -0.03966 | 1.99910 | 4.02357 | 0.01700 | 6.03966 |
| $\mathrm{C}_{16}$ | -0.19644 | 1.99918 | 4.17976 | 0.01750 | 6.19644 |
| $\mathrm{C}_{17}$ | -0.19295 | 1.99928 | 4.17524 | 0.01843 | 6.19295 |
| $\mathrm{C}_{18}$ | -0.20589 | 1.99928 | 4.18839 | 0.01821 | 6.20589 |
| $\mathrm{C}_{19}$ | -0.18278 | 1.99925 | 4.16581 | 0.01772 | 6.18278 |
| $\mathrm{C}_{20}$ | -0.26257 | 1.99915 | 4.24604 | 0.01737 | 6.26257 |
| $\mathrm{H}_{21}$ | 0.36029 | 0.00000 | 0.63847 | 0.00124 | 0.63971 |
| $\mathrm{H}_{22}$ | 0.19874 | 0.00000 | 0.79975 | 0.00151 | 0.80126 |
| $\mathrm{H}_{23}$ | 0.22161 | 0.00000 | 0.77691 | 0.00148 | 0.77839 |
| $\mathrm{H}_{24}$ | 0.24164 | 0.00000 | 0.75667 | 0.00168 | 0.75836 |
| $\mathrm{H}_{25}$ | 0.19444 | 0.00000 | 0.80453 | 0.00103 | 0.80556 |
| $\mathrm{H}_{26}$ | 0.19987 | 0.00000 | 0.79587 | 0.00426 | 0.80013 |
| $\mathrm{H}_{27}$ | 0.20543 | 0.00000 | 0.79347 | 0.00111 | 0.79457 |
| $\mathrm{H}_{28}$ | 0.19945 | 0.00000 | 0.79957 | 0.00098 | 0.80055 |
| $\mathrm{H}_{29}$ | 0.18204 | 0.00000 | 0.81713 | 0.00084 | 0.81796 |
| $\mathrm{H}_{30}$ | 0.20399 | 0.00000 | 0.79507 | 0.00094 | 0.79601 |
| $\mathrm{H}_{31}$ | 0.20450 | 0.00000 | 0.79468 | 0.00081 | 0.79550 |
| $\mathrm{H}_{32}$ | 0.20517 | 0.00000 | 0.79407 | 0.00076 | 0.79483 |
| $\mathrm{H}_{33}$ | 0.20581 | 0.00000 | 0.79338 | 0.00082 | 0.79419 |
| $\mathrm{H}_{34}$ | 0.22115 | 0.00000 | 0.77771 | 0.00114 | 0.77885 |
| $\mathrm{H}_{35}$ | 0.20573 | 0.00000 | 0.79329 | 0.00098 | 0.79427 |
| $\mathrm{H}_{36}$ | 0.20709 | 0.00000 | 0.79212 | 0.00079 | 0.79291 |
| $\mathrm{H}_{37}$ | 0.20733 | 0.00000 | 0.79191 | 0.00076 | 0.79267 |
| $\mathrm{H}_{38}$ | 0.20641 | 0.00000 | 0.79281 | 0.00078 | 0.79359 |
| $\mathrm{H}_{39}$ | 0.22323 | 0.00000 | 0.77450 | 0.00227 | 0.77677 |
| $\mathrm{Core}^{\text {Valence }}$ | 39.9854 | $99.9637 \%$ of 40 |  |  |  |
| Rydberg | 0.38873 | $0.2738 \%$ of 142 |  |  |  |
|  |  |  |  |  |  |

the second-order perturbation interaction ${ }^{29-32}$ energy $E(2)$. For each donor (i) and acceptor (j), the stabilisation energy $E(2)$ associated with the delocalization $\mathrm{i} \rightarrow \mathrm{j}$ is estimated as :

$$
E(2)=\Delta E_{i j}=q_{i} \frac{F(i j)^{2}}{\varepsilon_{j}-\varepsilon_{i}}
$$

where $q_{i}$ is the donor orbital occupancy, $\varepsilon_{I}$ and $\varepsilon_{j}$ are the diagonal elements and $F(i, j)$ is the off diagonal NBO Fock matrix element. The NBO analysis
provides an efficient method for studying intermolecular and intramolecular bonding. It also provides a convenient basis for intermolecular charge transfer (ICT) or conjugative interactions in molecular system. Table 8 presents the second order perturbation energies (often called as stabilizations energies or interaction energies) of most interacting NBO of MDPO. The second order perturbation energies correspond to the hyper conjugative interactions of title compound such as LP (2) $\mathrm{O} 7 \rightarrow \mathrm{BD}^{*}(1) \mathrm{C}_{3}-\mathrm{C}_{4}$ and $\mathrm{LP}(2) \mathrm{O}_{7} \rightarrow \mathrm{BD}^{*}(1) \mathrm{C}_{4}-\mathrm{C}_{5}$ that

Table 7 - Occupancies and energies of lone pair orbitals (LP) and anti-bonding ( $\mathrm{BD}^{*}$ ) molecular orbitals of MDPO

are considerably very large with 25.73 and $22.64 \mathrm{kJmol}^{-1}$, respectively. The interactions such as $\mathrm{LP}(1) \mathrm{N}_{1} \rightarrow \mathrm{BD}^{*}(1) \mathrm{C}_{6}-\mathrm{H}_{26}$ and LP (1) $\mathrm{N}_{1} \rightarrow \mathrm{BD}^{*}(1)$ $\mathrm{C}_{2}-\mathrm{C}_{15}$ are little higher than the rest of the interactions as presented in Table 8. These hyper conjugative interactions are the most responsible ones for stability of title compound.

### 9.4 Electron contribution in s-type and p-type subshells

NBO analysis of title compound is performed to estimate the delocalisation patterns of electron density(ED) from the principal occupied Lewis-type (bond or lone pair) orbitals to unoccupied non-Lewis (anti-bonding or Rydberg) orbitals. The list of occupancies and energies of most interacting NBOs along with their percentage of hybrid atomic orbitals is listed in Table 9. The percentage of hybrid atomic orbitals of oxygen lone pair atom $\mathrm{O}_{7}$ and nitrogen lone pair atom $\mathrm{N}_{1}$ shows that $\mathrm{O}_{7}$ is partially contributed to both s-type and p-type subshells, while $\mathrm{N}_{1}$ is predominantly contributed to p-type subshell. In contrast, all the anti-bonding orbitals of title compound

Table 9 - Natural atomic orbital occupancies of most
interacting(lone pair and anti-bonding) NBOs of MDPO

| Parameters | Occupancies | Hybrid | AO(\%) |
| :---: | :---: | :---: | :---: |
| LP (1) $\mathrm{N}_{1}$ | 1.93438 | spp ${ }^{4.39}$ | $\mathrm{s}(18.55) \mathrm{p}(81.45)$ |
| LP (1) $\mathrm{O}_{7}$ | 1.97572 | $\mathrm{sp}^{0.76}$ | $\mathrm{s}(56.95) \mathrm{p}(43.05)$ |
| $\mathrm{BD}^{*}(1)$ | 0.02236 | $\mathrm{sp}^{2.40}\left(\mathrm{~N}_{1}\right)$ | $\mathrm{s}(29.41) \mathrm{p}(70.59)$ |
| $\mathrm{N}_{1}-\mathrm{C}_{2}$ |  | $\mathrm{sp}^{3.45}\left(\mathrm{C}_{2}\right)$ | $\mathrm{s}(22.45) \mathrm{p}(77.55)$ |
| $\mathrm{BD}^{*}(1)$ | 0.02414 | $\mathrm{sp}^{2.30}\left(\mathrm{~N}_{1}\right)$ | $\mathrm{s}(30.28) \mathrm{p}(69.72)$ |
| $\mathrm{N}_{1}-\mathrm{C}_{6}$ |  | $\mathrm{sp}^{3.566}\left(\mathrm{C}_{6}\right)$ | $\mathrm{s}(21.93) \mathrm{p}(78.07)$ |
| $\mathrm{BD}^{*}(1)$ | 0.02783 | $\mathrm{sp}^{2.75}\left(\mathrm{C}_{2}\right)$ | $\mathrm{s}(26.68) \mathrm{p}(73.32)$ |
| $\mathrm{C}_{2}-\mathrm{C}_{3}$ |  | $\mathrm{sp}^{2.658}\left(\mathrm{C}_{3}\right)$ | s(27.14) p(72.86) |
| BD** ${ }^{\text {(1) }}$ | 0.02999 | $\mathrm{sp}^{2.52}\left(\mathrm{C}_{2}\right)$ | $\mathrm{s}(28.43) \mathrm{p}(71.57)$ |
| $\mathrm{C}_{2}-\mathrm{C}_{15}$ |  | $\mathrm{sp}^{2.13}\left(\mathrm{C}_{15}\right)$ | s(31.97) p(68.03) |
| $\mathrm{BD}^{*}(1)$ | 0.05258 | $\mathrm{sp}^{3.03}\left(\mathrm{C}_{3}\right)$ | $\mathrm{s}(24.81) \mathrm{p}(75.19)$ |
| $\mathrm{C}_{3}-\mathrm{C}_{4}$ |  | $\mathrm{sp}^{1.695}{ }^{\text {27 }}$ ( $\mathrm{C}_{4}$ ) | $\mathrm{s}(37.15) \mathrm{p}(62.85)$ |
| $\mathrm{BD}^{*}(1)$ | 0.01009 | $\mathrm{sp}^{2.75}\left(\mathrm{C}_{3}\right)$ | $\mathrm{s}(26.66) \mathrm{p}(73.34)$ |
| $\mathrm{C}_{3}-\mathrm{C}_{8}$ |  | $\mathrm{sp}^{2.41}\left(\mathrm{C}_{8}\right)$ | $\mathrm{s}(29.30) \mathrm{p}(70.70)$ |
| BD* ${ }^{*}$ (1) | 0.04249 | $\mathrm{sp}^{2.14}\left(\mathrm{C}_{4}\right)$ | $\mathrm{s}(31.81) \mathrm{p}(68.19)$ |
| $\mathrm{C}_{4}-\mathrm{C}_{5}$ |  | $\mathrm{sp}^{2.77}\left(\mathrm{C}_{5}\right)$ | $\mathrm{s}(26.49) \mathrm{p}(73.51)$ |
| BD* ${ }^{\text {(1) }}$ | 0.01229 | $\mathrm{sp}^{2.23}\left(\mathrm{C}_{4}\right)$ | $\mathrm{s}(30.98) \mathrm{p}(69.02)$ |
| $\mathrm{C}_{4}-\mathrm{O}_{7}$ |  | $\mathrm{sp}^{1.33}\left(\mathrm{O}_{7}\right)$ | $\mathrm{s}(42.83) \mathrm{p}(57.17)$ |
| $\mathrm{BD}^{*}(1)$ | 0.02336 | $\mathrm{sp}^{2.72}\left(\mathrm{C}_{5}\right)$ | $\mathrm{s}(26.89) \mathrm{p}(73.11)$ |
| $\mathrm{C}_{5}-\mathrm{C}_{6}$ |  | $\mathrm{sp}^{2.87}\left(\mathrm{C}_{6}\right)$ | $\mathrm{s}(25.85) \mathrm{p}(74.15)$ |
| $\mathrm{BD}^{*}(1)$ | 0.02540 | $\mathrm{sp}^{2.49}\left(\mathrm{C}_{6}\right)$ | s(28.62) p(71.38) |
| $\mathrm{C}_{6}{ }^{-} \mathrm{C}_{9}$ |  | $\mathrm{sp}^{2.11}\left(\mathrm{C}_{9}\right)$ | s(32.13) p(67.87) |
| BD* ${ }^{\text {(1) }}$ | 0.02106 | sp ${ }^{1.90}\left(\mathrm{C}_{9}\right)$ | s(34.54) p(65.46) |
| $\mathrm{C}_{9}-\mathrm{C}_{10}$ |  | $\mathrm{sp}^{1.78}\left(\mathrm{C}_{10}\right)$ | s(35.91) p(64.09) |
| $\mathrm{BD}^{*}(1)$ | 0.02327 | $\mathrm{sp}^{2.000}\left(\mathrm{C}_{9}\right)$ | $\mathrm{s}(33.33) \mathrm{p}(66.67)$ |
| $\mathrm{C}_{9}-\mathrm{C}_{14}$ |  | $\mathrm{sp}^{1.80}\left(\mathrm{C}_{14}\right)$ | $\mathrm{s}(35.66) \mathrm{p}(64.34)$ |
| $\mathrm{BD}^{*}(1)$ | 0.01238 | $\mathrm{sp}^{1.83}\left(\mathrm{C}_{10}\right)$ | $\mathrm{s}(35.35) \mathrm{p}(64.65)$ |
| $\mathrm{C}_{10}-\mathrm{C}_{11}$ |  | $\mathrm{sp}^{1.81}\left(\mathrm{C}_{11}\right)$ | $\mathrm{s}(35.56) \mathrm{p}(64.44)$ |
| $\mathrm{BD}^{*}(1)$ | 0.01348 | $\mathrm{sp}^{1.81}\left(\mathrm{C}_{11}\right)$ | $\mathrm{s}(35.62) \mathrm{p}(64.38)$ |
| $\mathrm{C}_{11}{ }^{\text {+ }}$ (12 |  | $\mathrm{sp}^{1.82}\left(\mathrm{C}_{12}\right)$ | $\mathrm{s}(35.51) \mathrm{p}(64.49)$ |
| $\mathrm{BD}^{*}(1)$ | 0.01351 | $\mathrm{sp}^{1.81}\left(\mathrm{C}_{12}\right)$ | $\mathrm{s}(35.55) \mathrm{p}(64.45)$ |
| $\mathrm{C}_{12}-\mathrm{C}_{13}$ |  | $\mathrm{sp}^{1.82}\left(\mathrm{C}_{13}\right)$ | $\mathrm{s}(35.47) \mathrm{p}(64.53)$ |
| $\mathrm{BD}^{*}(1)$ | 0.01284 | $\mathrm{sp}^{1.80}\left(\mathrm{C}_{13}\right)$ | s(35.73) p(64.27) |
| $\mathrm{C}_{13}-\mathrm{C}_{14}$ |  | $\mathrm{sp}^{1.85}\left(\mathrm{C}_{14}\right)$ | s(35.13) p(64.87) |
| $\mathrm{BD}^{*}(1)$ | 0.02079 | $\mathrm{sp}^{1.90}\left(\mathrm{C}_{15}\right)$ | $\mathrm{s}(34.44) \mathrm{p}(65.56)$ |
| $\mathrm{C}_{15}-\mathrm{C}_{16}$ |  | $\operatorname{sp}^{1.79}\left(\mathrm{C}_{16}\right)$ | $\mathrm{s}(35.88) \mathrm{p}(64.12)$ |
| $\mathrm{BD}^{*}(1)$ | 0.02516 | $\mathrm{sp}^{1.98}\left(\mathrm{C}_{15}\right)$ | $\mathrm{s}(33.55) \mathrm{p}(66.45)$ |
| $\mathrm{C}_{15}-\mathrm{C}_{20}$ |  | $\mathrm{sp}^{1.87}\left(\mathrm{C}_{20}\right)$ | $\mathrm{s}(34.81) \mathrm{p}(65.19)$ |
| BD* ${ }^{\text {(1) }}$ | 0.01252 | $\mathrm{sp}^{1.84}\left(\mathrm{C}_{16}\right)$ | s(35.23) p(64.77) |
| $\mathrm{C}_{16}{ }^{-} \mathrm{C}_{17}$ |  | $\mathrm{sp}^{1.81}\left(\mathrm{C}_{17}\right)$ | $\mathrm{s}(35.55) \mathrm{p}(64.45)$ |
| $\mathrm{BD}^{*}(1)$ | 0.01329 | $\mathrm{sp}^{1.81}\left(\mathrm{C}_{17}\right)$ | $\mathrm{s}(35.55) \mathrm{p}(64.45)$ |
| $\mathrm{C}_{17}-\mathrm{C}_{18}$ |  | $\mathrm{sp}^{1.81}{ }^{\text {(82 }}$ ( $\mathrm{C}_{18}$ ) | $\mathrm{s}(35.55) \mathrm{p}(64.45)$ |
| $\mathrm{BD}^{*}(1)$ | 0.01302 | $\mathrm{sp}^{1.88}\left(\mathrm{C}_{18}\right)$ | $\mathrm{s}(35.47) \mathrm{p}(64.53)$ |
| $\mathrm{C}_{18}{ }^{-} \mathrm{C}_{19}$ |  | $\mathrm{sp}^{1.83}\left(\mathrm{C}_{19}\right)$ | $\mathrm{s}(35.38) \mathrm{p}(64.62)$ |
| $\mathrm{BD}^{*}(1)$ | 0.01646 | $\mathrm{sp}^{1.80}\left(\mathrm{C}_{19}\right)$ | $\mathrm{s}(35.78) \mathrm{p}(64.22)$ |
| $\mathrm{C}_{19}-\mathrm{C}_{20}$ |  | $\mathrm{sp}^{1.85}\left(\mathrm{C}_{20}\right)$ | $\mathrm{s}(35.04) \mathrm{p}(64.96)$ |

are mainly contributed to p-type subshell, except in the $\mathrm{BD}^{*}(1) \mathrm{C}_{4}-\mathrm{O}_{7}$ orbital which shows that $\mathrm{O}_{7}$ is partially contributed to both s-type and p-type subshell, as stated in Table 9.

## 10 NLO Properties

Polarizabilities and hyperpolarizabilities characterize the response of a system in an applied
electric field. They determine not only the strength of molecular interactions as well as the cross-sections of different scattering and collision processes, but also the non-linear optical properties (NLO) of the system ${ }^{33}$. The second-order polarizability or first hyperpolarizability $\beta$, dipole moment $\mu$ and polarizability $\alpha$ are calculated using B3LYP/6$311++G(d, p)$ basis set on the basis of the finite-field approach.

In the presence of an external electric field (E), the energy of the system is a function of the electric field. First hyperpolarizability is a third-rank tensor that can be described by a $3 \times 3 \times 3$ matrix. The 27 components of the 3 D matrix can be reduced to 10 components because of the Kleinman symmetry ${ }^{34}$. The components of $\beta$ are defined as the coefficients in the Taylor series expansion of energy in an external electric field.

When an external electric field is weak and homogeneous, Taylor series expansion becomes:

$$
E=E^{0}-\frac{\mu_{i} F_{i}}{1!}-\frac{\alpha_{i j} F_{i} F_{j}}{2!}-\frac{\beta_{i j k} F_{i} F_{j} F_{k}}{3!}-\frac{\gamma_{i j k l} F_{i} F_{j} F_{k} F_{l}}{4!}
$$

where $E$ is the energy of the unperturbed molecules, $F_{i}$ is the field at origin and $\mu_{i}, \alpha_{i j}, \beta_{i j k}$ and $\gamma_{i j k l}$ are the components of dipole moment, polarizability, first hyperpolarizabilities and the second hyperpolarizeabilities, respectively. The complete equations for calculating the magnitude of total static dipole moment $\mu$, the mean polarizability $\alpha_{0}$, the anisotropy of the polarizability $\Delta \alpha$ and the mean first polarizability $\beta_{\text {tot }}$ using $x, y$ and $z$ components from Gaussian 09 output is as follows:

Dipole moment, $\mu=\left(\mu_{x}{ }^{2}+\mu_{y}{ }^{2}+\mu_{z}{ }^{2}\right)^{1 / 2}$
Mean polarisability $\alpha_{o}=\frac{\alpha_{x x}+\alpha_{y y}+\alpha_{z z}}{3}$
Anisotropic polarisability

$$
\begin{aligned}
\Delta \alpha= & 2^{-1 / 2}\left[\left(\alpha_{x x}-\alpha_{y y}\right)^{2}+\left(\alpha_{y y}-\alpha_{z z}\right)^{2}\right. \\
& \left.+\left(\alpha_{z z}-\alpha_{x x}\right)^{2}+6 \alpha_{x z}{ }^{2}\right]^{1 / 2}
\end{aligned}
$$

first-order polarisability $\beta_{t o t}=\left(\beta_{x}{ }^{2}+\beta_{y}{ }^{2}+\beta_{z}{ }^{2}\right)^{1 / 2}$ and
$\beta_{x}=\beta_{x x x}+\beta_{y y y}+\beta_{z z z}$
$\beta_{y}=\beta_{y y y}+\beta_{x x y}+\beta_{y z z}$
$\beta_{z}=\beta_{z z z}+\beta_{x x z}+\beta_{y y z}$

Table 10 - Electric dipole moment $\mu$ (Debye), mean polarizability $\alpha_{o}\left(10^{-22} \mathrm{esu}\right)$, anisotropy polarizability $\Delta \alpha\left(10^{-25}\right.$ esu) and first hyperpolarizability $\beta_{\text {tot }}\left(10^{-31} \mathrm{esu}\right)$ for MDPO

| Parameters | Values | Parameters | Values |
| :---: | :---: | :---: | :---: |
| $\mu_{x}$ | 0.3097 | $\beta_{x x x}$ | -5.8989 |
| $\mu_{y}$ | -3.7455 | $\beta_{y y y}$ | -75.5792 |
| $\mu_{z}$ | -0.9297 | $\beta_{z z z}$ | 0.3078 |
| $\mu$ | 3.8715 | $\beta_{x y y}$ | 11.4864 |
| $\alpha_{x x}$ | -110.6647 | $\beta_{x x y}$ | -36.6550 |
| $\alpha_{x y}$ | -0.5493 | $\beta_{x x z}$ | -19.4291 |
| $\alpha_{x z}$ | -2.0401 | $\beta_{x z z}$ | -6.0989 |
| $\alpha_{y y}$ | -139.3812 | $\beta_{y z z}$ | 2.8540 |
| $\alpha_{y z}$ | -1.5112 | $\beta_{y y z}$ | 11.7813 |
| $\alpha_{z z}$ | -113.4516 | $\beta_{x y z}$ | -2.5770 |
| $\alpha_{o}$ | -121.16583 | $\beta_{t o t}$ | 109.6273 |
| $\Delta \alpha$ | 27.6560 |  |  |

The polarizabilities and hyperpolarizability are reported in atomic units (au). The hyperpolarizability $\beta$, dipole moment $\mu$ and polarizability $\alpha$ of MDPO are presented in Table 10. The calculated value of dipole moment was found to be 3.8715 Debye. The highest value of dipole moment is observed for component $\mu_{x}$. In this direction, this value is equal to 0.3097 Debye. The calculated polarizability and anisotropy of the polarizability of MDPO are $-121.16583 \times 10^{-22}$ esu and $27.6560 \times 10^{-25}$ esu, respectively. The magnitude of the molecular hyperpolarizability $\beta$ is found to be $109.6273 \times 10^{-31}$ esu and is one of the important key factors in a NLO system ${ }^{35}$. The calculated value of $\beta$ suggests the usefulness of the piperidine as catalyst in chemical reactions to enhance NLO character. The dipole moment and first hyperpolarizability of title molecule can be compared with those of urea ( $\mu$ and $\beta$ of urea are 1.525686 Debye and $0.780324 \times 10^{-30}$ esu obtained by B3LYP/6-311++G(d,p) method). Since urea is one of the prototypicalmolecules used in the study of the NLO properties of molecular systems, it was used frequently as a threshold value for comparative purpose.

## 11 Conclusions

A complete vibrational analysis has been carried out for MDPO using FT-IR and Raman spectroscopy. Assignments of the vibrational spectra have been facilitated by DFT calculation. A good correlation was found between the computed and experimental wavenumbers.The molecular structural parameters like bond length, bond angle, torsional angle and dihedral angle have been determined from ab-initio
and DFT calculations using 6-311++G(d,p) basis set. Mulliken charges of MDPO at different levels were calculated and the results discussed. HOMO, LUMO energies and HOMO-LUMO energy gap are calculated as 4.9427 eV . The delocalization pattern of charge and electron densities of MDPO molecule have been explained by performing molecular orbital simulations at HF method with 6-311 ++G basis set. The stabilization of the structure has been identified by second order perturbation energy calculations. The calculation of first hyperpolarizability gives MDPOs utility as catalyst to increase NLO properties. The UV analysis gives the electronic spectrum of MDPO that has revealed the allowed and forbidden transitions with solvent effects.

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